



Subject: Electronic Devices and Circuits

(a) Course Objectives:

- To provide an overview of the principles and operation of electronic devices.
- To explore use of electronic devices for various applications in electronic circuits.
- To analyze various electronic circuits.

(b) Course Outcomes(Proposed):

After successfully completing the course, the students will be able to

- **CO1:** Comprehend the knowledge of semiconductor devices(Diode, BJT, JFET, MOSFET, UJT), rectifiers, filters, amplifiers & oscillator circuits
- **CO2:** Understand basics of Diode, BJT, JFET, MOSFET, UJT, Rectifier, filters, Amplifiers, Oscillators with analysis of their characteristics and operational parameters.
- **CO3:** To understand Biasing, feedback concept, topologies and their applications.
- **CO4:** Implement and analyze various electronic circuits..



Subject: Electronic Devices and Circuits

Unit-2

Wave shaping : Analysis of RC low pass and high pass filters for sinusoidal, step, pulse, square signal. Analysis of clipping and clamping circuits using diodes



Unit-II: WAVE SHAPING CIRCUITS-

Lectures required	Topic	Books
	Wave shaping circuits	
L1-L3	RC low pass and high pass circuits-	T1,T2
L4-L5	Clippers-	T2, T1
L6-L7	Clampers	



Subject: Electronic Devices and Circuits

Unit2: WAVE SHAPING CIRCUITS

Part-I WAVE SHAPING CIRCUITS: RC CIRCUITS

- ✓ Definition of wave shaping circuit
- ✓ Purpose of wave shaping circuits
- ✓ Types of wave shaping circuits
- ✓ Analysis of High pass & low pass RC circuits

Part-II CLIPPER CIRCUITS

- ✓ Definition of Clipping circuit
- ✓ Purpose of Clipping circuits
- ✓ Types of Clipping circuits
- ✓ Analysis of Clipping circuits

Part-III CLAMPING CIRCUITS

- ✓ Definition of Clamping circuit
- ✓ Purpose of Clamping circuits
- ✓ Types of Clamping circuits
- ✓ Analysis of Clamping circuits



Waveshaping circuits

Prerequisite

- ❖ **Fundamentals of PN Junction Diode**
- ❖ **Biassing and Operation of the Diode**
- ❖ **VI Characteristics of Diode**
- ❖ **Ideal and Practical Parameters**
- ❖ **Basics of standard signals**
- ❖ **Basics about Electrical circuit elements
(R,L,C)**



Wave shaping circuits-

Wave shaping circuits means:

A process by which non-sinusoidal waveforms are altered in passing through the circuit elements (such as diodes, resistors, inductors, capacitors) is called wave shaping and circuit used for this purpose is referred as wave shaping circuits.

The wave shaping is used to perform following functions:

- i) To generate one wave from the other
- ii) To limit the voltage level of the waveform to some preset value and suppressing all other voltage levels in excess of the preset level
- iii) To cutoff the positive and negative portions of the input waveforms
- iv) To hold the waveform to a particular dc level

The wave shaping is important in most of the signal processing systems...



Wave shaping circuits

The wave shaping is performed by the circuits known as-

- **Low pass RC circuit(LPF, Integrators when $\tau \gg T$)**
- **High pass RC circuit(HPF, Differentiators when $\tau \ll T$)**
- Limiters circuits
- Clipper circuits
- Clamper circuits



Wave shaping circuits

The wave shaping is performed by the circuits known as-

- Low pass RC circuit(LPF, Integrators)- To generate a voltage, which increases or decreases linearly with time (ramp signal)
- High pass RC circuit(HPF,Differentiators)- To generate sharp narrow pulses either from rectangular waveforms or distorted pulse waveforms
- Limiters circuits-To limit the voltage level of the waveform to some preset value and suppressing all other voltage levels in excess of this preset levels, it is also called amplitude limiters
- Clipper circuits- To cut-off the positive and negative portion of an input waveforms
- Clamper circuits- It is used to hold or restore the waveform to a particular dc level or used to change average value of sinusoidal signal



Wave shaping circuits

Different non-sinusoidal signal wave shapes or waveforms used in signal processing systems

non-sinusoidal signal wave shapes or waveforms are nothing but any waveform whose shape is different from that of a standard **sinusoidal wave**

Important non-sinusoidal signal waveforms:

- Step waveforms
- **Pulse waveforms**
- **Square waveforms**
- Symmetrical square waveforms
- **Triangular waveforms**
- Saw tooth waveforms

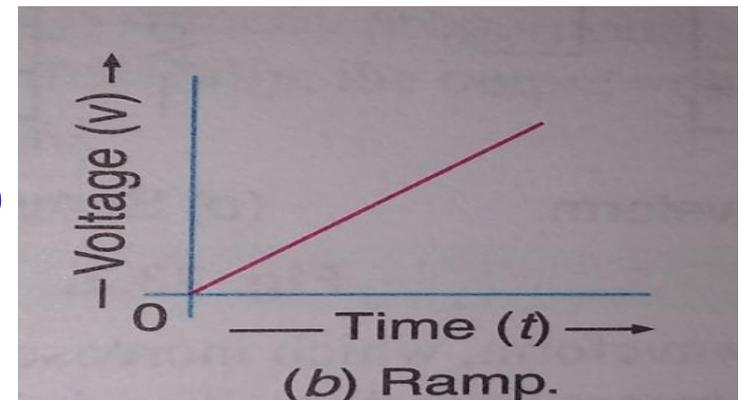
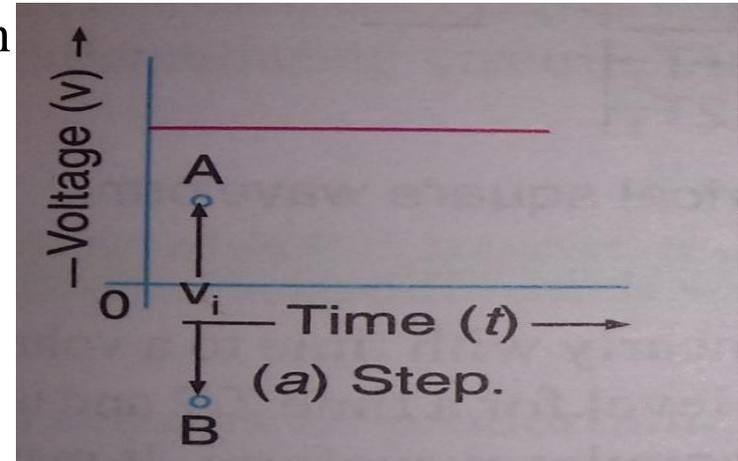
All these waveforms are a part of standard voltage or current signal such as step, ramp and exponential signals



Wave shaping circuits

Standard voltage or current signal such as-

- Step signal- maintains $V = 0$ for all times $t < 0$ and maintains voltage level V for all times $t > 0$ ($V = \text{some value}$), transition takes place at $t = 0$
- Ramp signal- maintains zero voltage level for $t < 0$ ($V = 0$) and increases linearly with time for $t > 0$ ($V = \alpha \cdot t$)

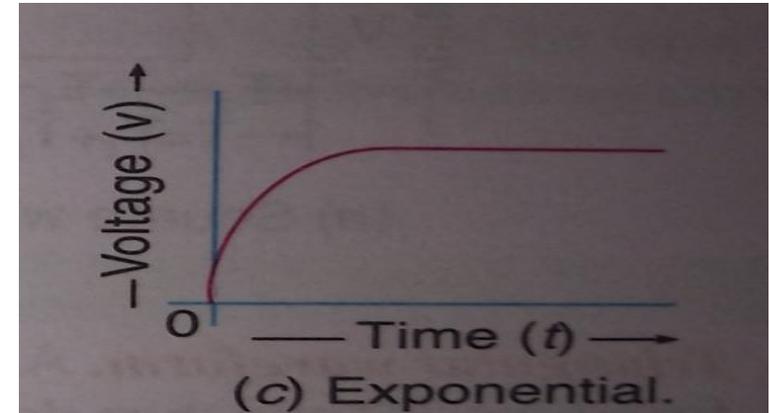




Wave shaping circuits

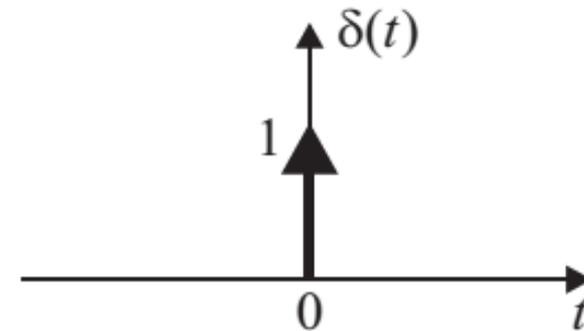
Standard voltage or current signal such as-

- Exponential signals- maintains $V = 0$ for $t < 0$ and increases nonlinearly with time for $t > 0$ that is $V = V_i e^{-t/\tau}$



- The impulse signal is a signal with infinite magnitude and zero duration, but with the unit area.

The unit impulse function is also known as the Dirac delta function.

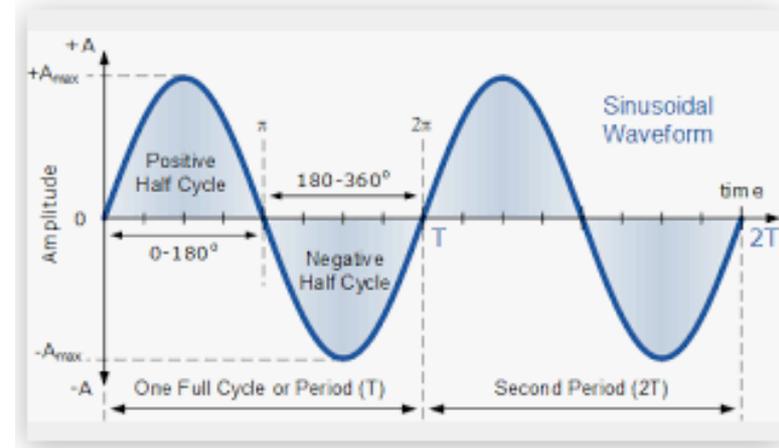


$$\delta(t) = \begin{cases} \infty & \text{at } t = 0 \\ 0 & \text{at } t \neq 0 \end{cases} \quad \text{and} \quad \int_{-\infty}^{\infty} \delta(t) dt = 1$$



Wave shaping circuits

Sinusoidal signals: Sine waves,



Important non-sinusoidal signal waveforms

- Pulse waveforms-
- Square waveforms-
- Symmetrical square
- Triangular waveforms-
- Sawtooth waveforms-

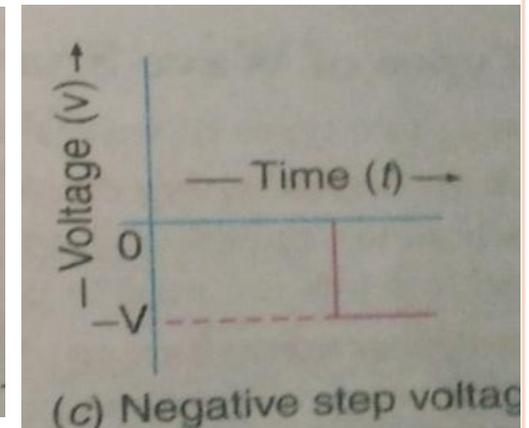
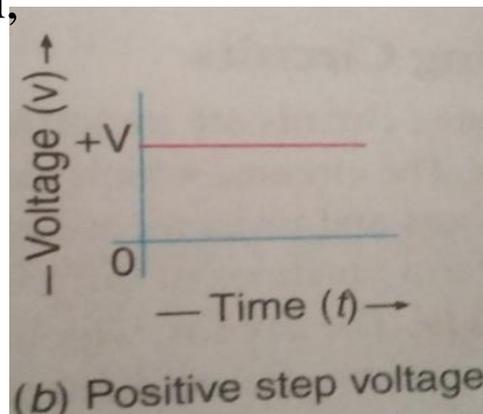
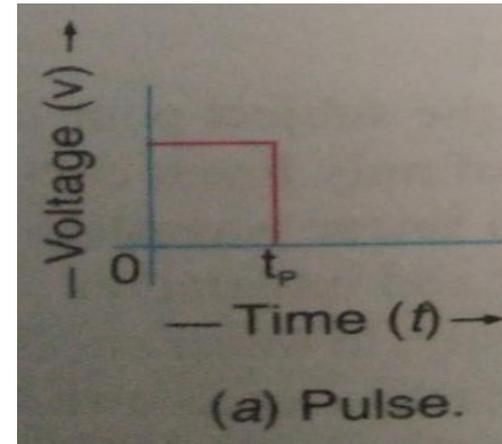


Wave shaping circuits

Important non-sinusoidal signal waveforms:

Pulse waveforms-

- Pulse amplitude is V and Pulse duration is t_p ,
- It is sum of the Positive and Negative step signal,
- used in communication, computers, defence equipments, etc



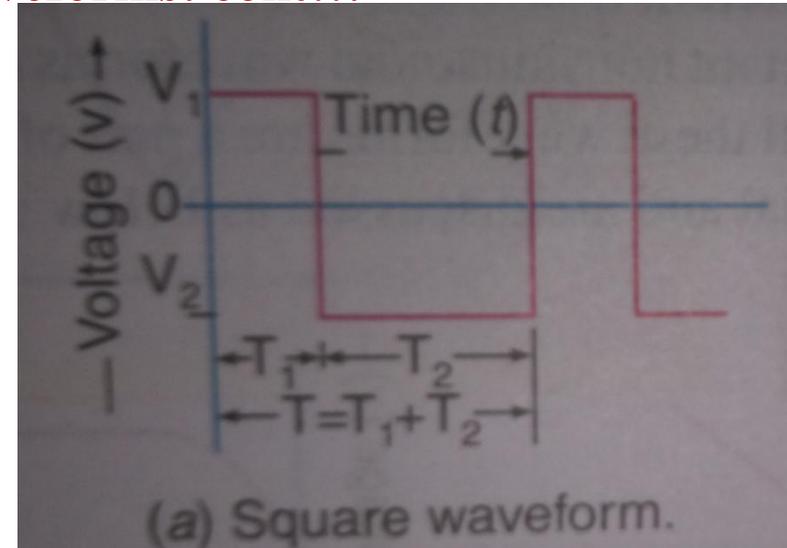


Wave shaping circuits

Important non-sinusoidal signal waveforms: cont...

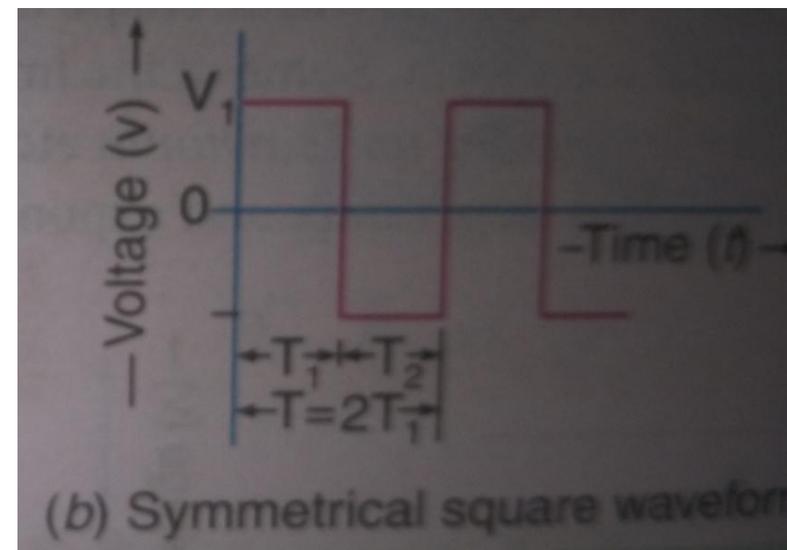
▪ Square waveforms-

It maintains one constant voltage level(+V for $t=T_1$) and another constant voltage level(-V₂ for $t=T_2$), it is a periodic waveform with $t=T_1+T_2$, used in Digital electronics circuits, radars, Television



▪ Symmetrical sq. waveforms

A square wave with $T_1=T_2=T/2$ and $V_1 = -V_2$, 50% duty cycle, it is a periodic waveform with $t=T_1+T_2$, used in Digital electronics circuits



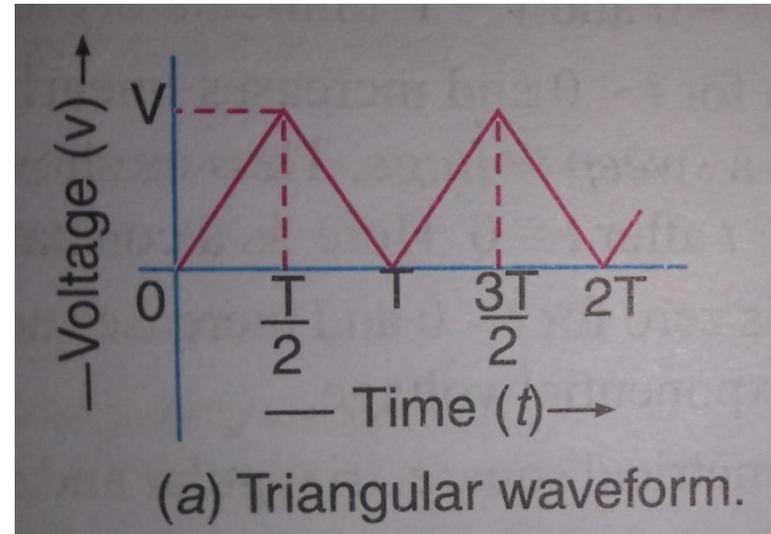


Wave shaping circuits

Important non-sinusoidal signal waveforms: cont...

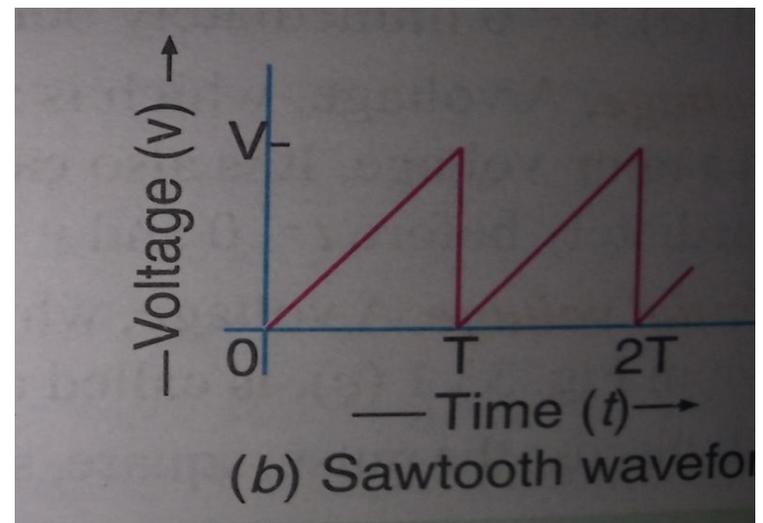
▪ **Triangular waveforms-**

Increases linearly with time to a voltage level V for $t=T/2$ and then decreases linearly to its original level for $t=T/2$, it is a sum of positive and negative ramp signal, it is a periodic waveform with $t=T_1+T_2$, use as timing circuits for electronics applications



▪ **Sawtooth waveforms-**

Increases linearly with time to a voltage level V for $t=T/2$ and then changes abruptly to its original level, it is a periodic waveform with $t=T_1$, it is referred as sweep or time base waveforms.





Types of Wave shaping circuits

Types of Wave shaping circuits: Linear & Non Linear

▪ Linear wave shaping circuits-

- The process in which the form of nonsinusoidal signals(such as step, pulse, square wave, ramp and exponential signals) gets altered by transmission through a linear circuit(described by linear differential equation, $V_o = Ri(t)+Ldi/dt+1/C \int idt$) is called linear wave shaping
- Using only linear circuit elements(Resistors, Capacitors, Inductors)
- Use to perform functions of Integration & differentiation

▪ Non linear wave shaping circuits-

- Using non linear circuit elements(diode, transistors)
- Use to perform functions of amplitude limiting, clipping and clamping



Subject: Electronic Devices and Circuits

Unit2: WAVE SHAPING CIRCUITS :Part-I

- ✓ Introduction to waveshaping circuits
- ✓ Definition of wave shaping circuit
- ✓ Purpose of wave shaping circuits
- ✓ Standard signal waveforms
- ✓ Derived signal waveforms
- ✓ Types of wave shaping circuits
- ✓ Analysis of High pass RC Circuits
- ✓ Analysis of Low pass RC circuits



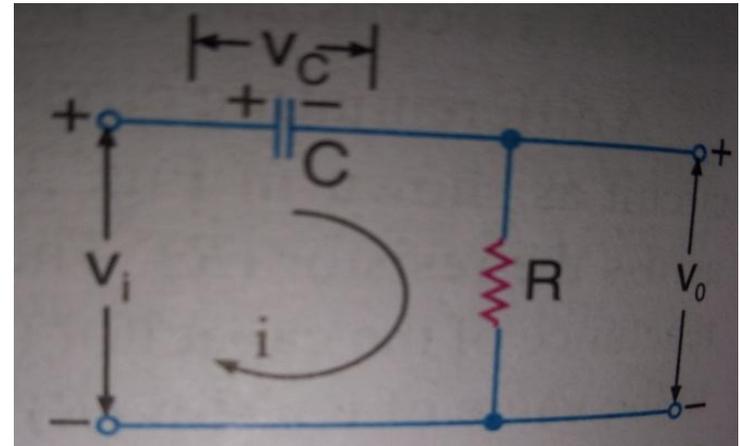
Linear wave shaping circuits

- **High pass RC circuits**

- High Pass Filter,
- as Differentiator- $\tau(RC) \ll T$

$$X_C = \frac{1}{2\pi fC}$$

- $f = 0, f = \infty$

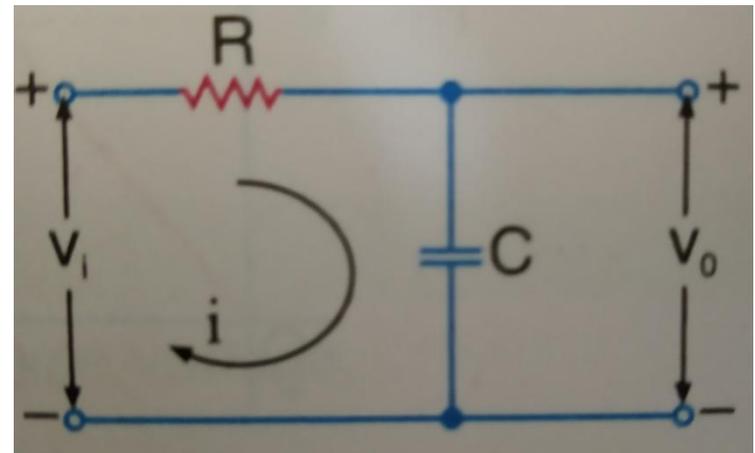


- **Low pass RC circuits**

- Low pass filters
- Use to perform functions of Integration, $\tau(RC) \gg T$

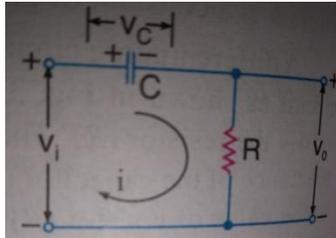
$$X_C = \frac{1}{2\pi fC}$$

- $f = 0, f = \infty$





Linear wave shaping circuits

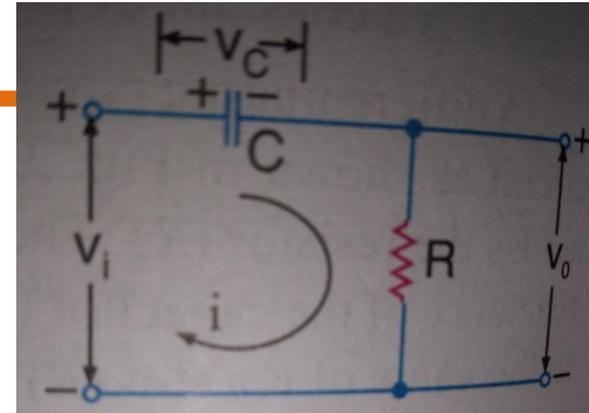


- **High pass RC circuits**
 - High Pass Filter,
 - as a Differentiator- $\tau (RC) \ll T$



Linear wave shaping circuits

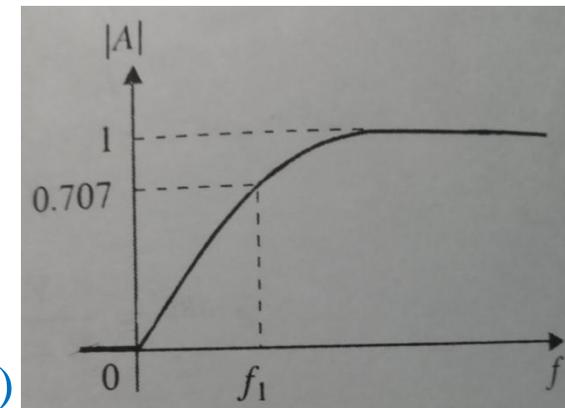
- **High pass RC circuits**
- **Low pass RC circuits**
- Referred as High pass and Low pass filters also
- Use to perform functions of differentiation & Integration



- 1. High pass RC circuits(hpf , use as differentiation ($\tau > T$, ie low f))

$$X_c = \frac{1}{2\pi f C}$$

- $f = 0, X_c \rightarrow \infty$ acts as open circuit or blocks dc signal and
- $f = \infty, X_c \rightarrow 0$ as short circuit, that is it pass ac components
- as f increases, X_c decreases, o/p and magnitude of gain increases
- High frequency components in the i/p signal appears at the o/p with less attenuation as compare to low frequency components
- For HF capacitor acts as a short circuit and all the i/p appears at the o/p such behavior of the circuit referrers as **High pass filter (HPF)**





High pass RC circuits: Sinusoidal Input

1. Sinusoidal Input

Expression for the lower cutoff frequency-

- $V_i = V_m \sin \omega t$
- $i = V_i / (R - jX_c)$
- $V_o = iR = V_i * R / (R - jX_c)$

$$|A| = \left| \frac{V_o}{V_i} \right| = \frac{R}{R - jX_c} = \frac{1}{1 - jX_c / R}$$

$$\left| \frac{V_o}{V_i} \right| = |A| = \frac{1}{\sqrt{1 + (X_c / R)^2}}$$

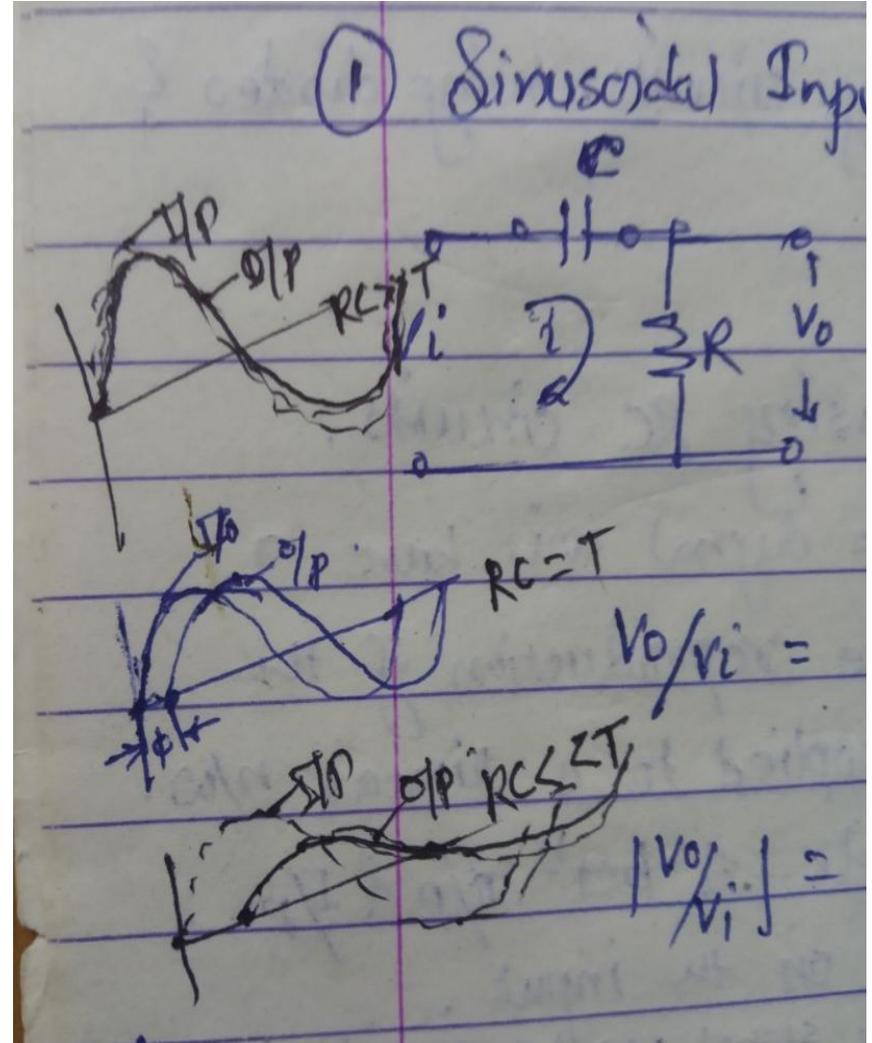
$$= \frac{1}{\sqrt{1 + (f_1 / f)^2}}$$

$$\theta = \tan^{-1} \frac{f_1}{f}$$

$$f_1 = \frac{1}{2\pi RC}$$

3db

lower cutoff freq.





High pass circuits: Step Input

2. Step Input

$V_i = 0, t < 0$ and $V_i = V, t > 0$

The transition between two voltage levels takes place at $t = 0$ Voltages at ($t=0+, t=0-$)

The response of High pass RC circuit is exponential with $RC = \tau$ and

$$V_0 = B_1 + B_2 e^{-t/\tau}$$

Constant B_1 - steady state value of V_0 as $t \rightarrow \infty$,

$$V_0 = B_1 = V_f$$

Constant B_2 derived from

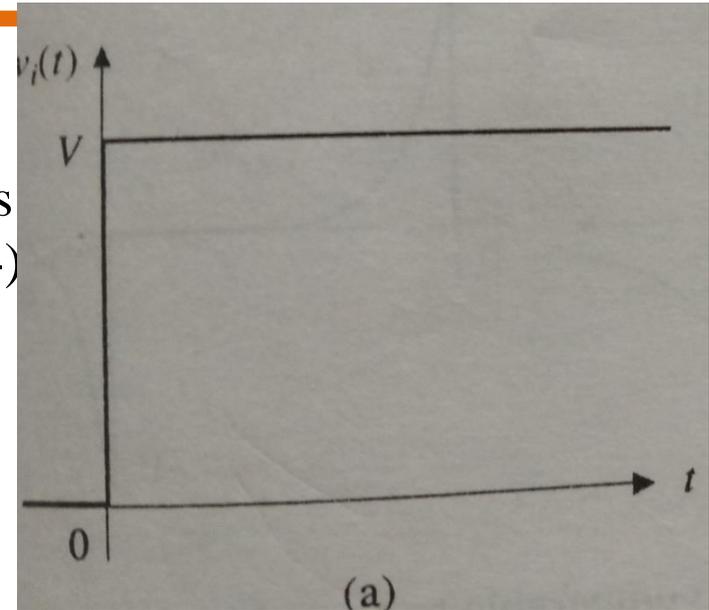
The initial value of V_0 at $t=0$

$$V_0 = V_i = B_1 + B_2$$

$$B_2 = V_i - V_f$$

$$V_0 = V_f + (V_i - V_f) e^{-t/\tau}$$

at steady state $V_0 = V e^{-t/\tau}$





High pass circuits

cont...

i. Capacitor C blocks DC and input is constant for $t > 0$, therefore $V_o = V_f = 0$

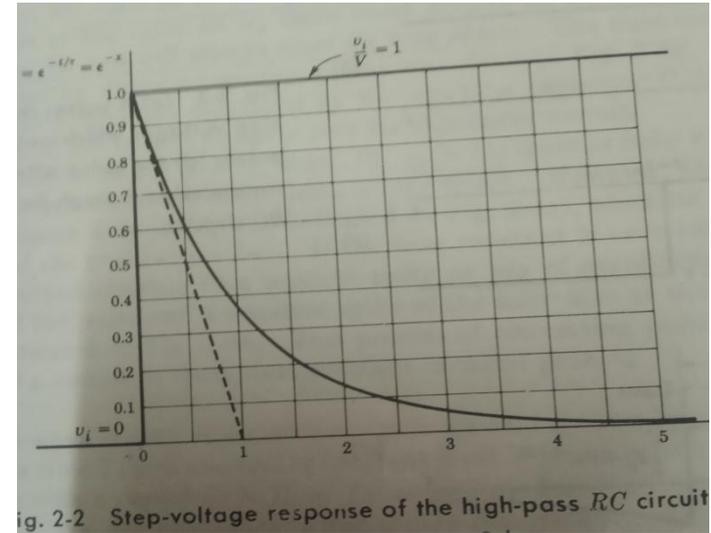
ii. Voltage across capacitor V_c

$$V_c = \frac{1}{C} \int_0^{t_1} i dt$$

iii. At $t=0$ V_i changes abruptly from 0 to V value and hence output must also changes abruptly by this same amount

iv. Initially capacitor is fully uncharged

Therefore $V_0 = V_{\text{initial}} = 0$, at $t = 0+$ $V_i = V$



The response of High pass RC circuit is exponential with $RC = \tau$

and $V_0 = V_f + (V_i - V_f) e^{-t/\tau}$

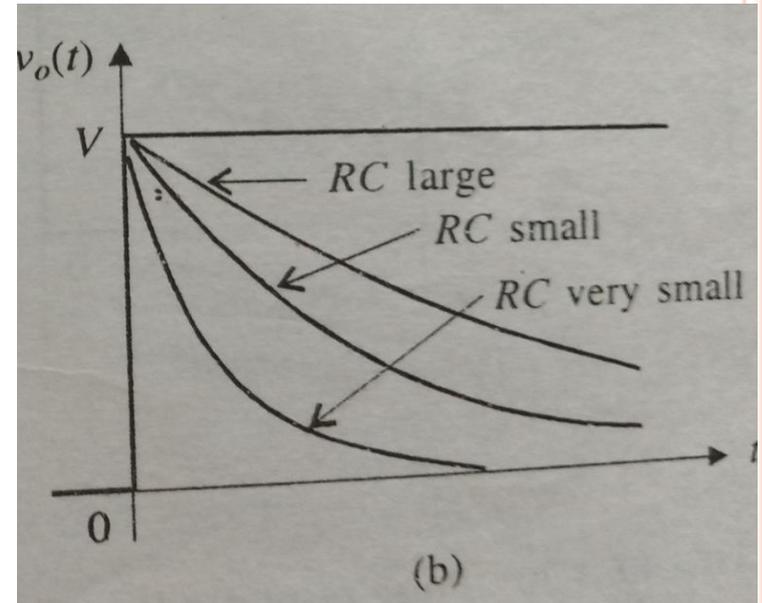
Therefore $V_0 = 0 + (V - 0) e^{-t/\tau}$ so $V_0 = V e^{-t/\tau}$



High pass circuits

cont...

- i. $RC \gg$
- ii. RC comparable
- iii. $RC \ll$



The response of High pass RC circuit is exponential with $RC = \tau$

Initially capacitor is fully uncharged

Therefore $V_0 = V_{\text{initial}} = 0$, at $t = 0+$ $V_i = V$

$$V_0 = V_f + (V_i - V_f) e^{-t/\tau}$$

$$\text{Therefore } V_0 = 0 + (V - 0) e^{-t/\tau} \text{ so } V_0 = V e^{-t/\tau}$$



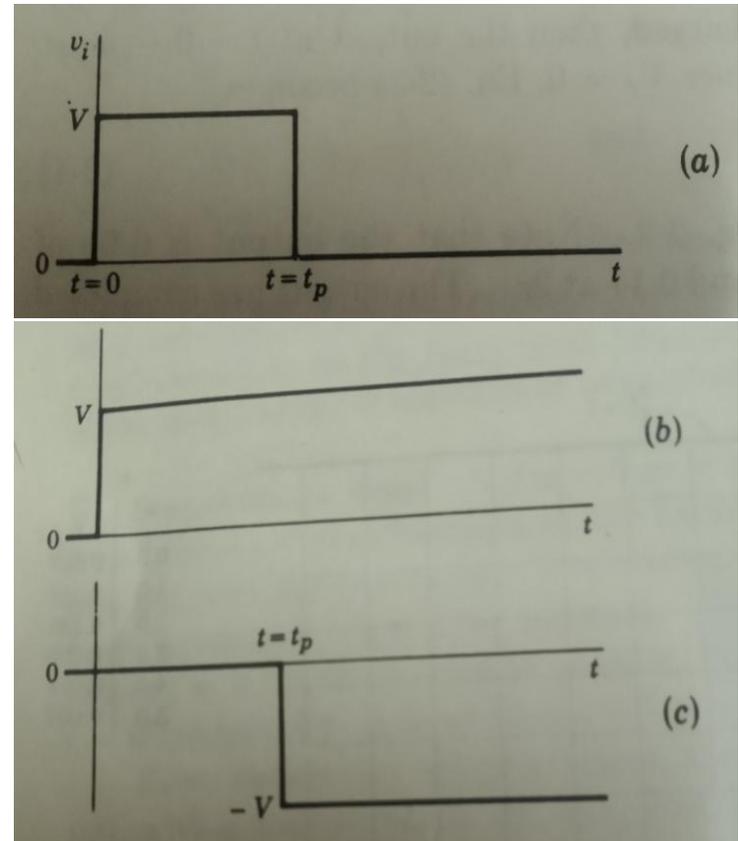
High pass circuits: Pulse Input

3. Pulse Input

- Pulse with Amplitude and Pulse duration t_p
- It is the combination of +ve and Negative Step input

or

Pulse input signal is the Sum of +V step voltage whose discontinuity occurs at $t=0$ and $-V$ step voltage whose discontinuity occurs $t= t_p$





High pass circuits: Pulse Input

3. cont....

- pulse input is applied to High pass RC circuit then Response

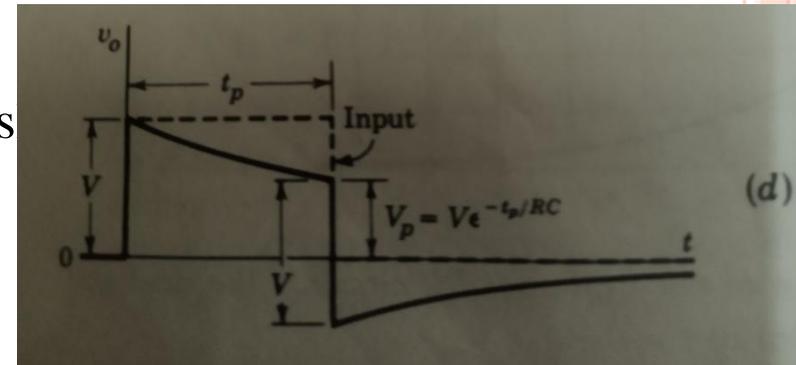
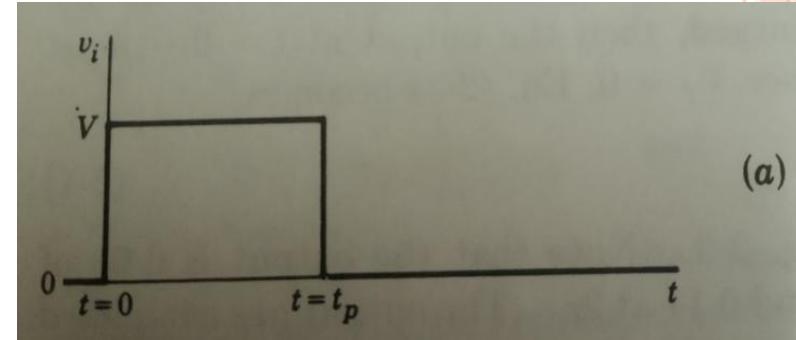
- i) for $t < t_p$ is similar to that for step input voltage

$$V_0 = Ve^{-t/\tau}$$

$$= Ve^{-t_p/\tau} = V_p \text{ at } t = t_p$$

- ii) at the end of pulse i/p falls abruptly by an amount V but the capacitor voltage cannot change instantaneous finite current flow therefore output must drop by same amount ie V at $t = t_p$, $V_0 = V_p - V$ ($V > V_p$)

- iii) V_0 is negative and then it decreases exponentially to zero with $V_0 = V(e^{-t_p/RC} - 1) = Ve^{-(t-t_p)/RC}$



$$V_C = \frac{1}{C} \int_0^{t_1} i dt$$



High pass circuits: Pulse Input

3. cont....

- Pulse input is applied to High pass RC circuit then Response for Various Circuit Time constant RC

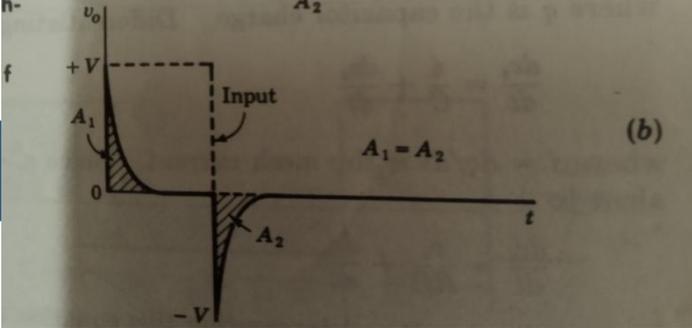
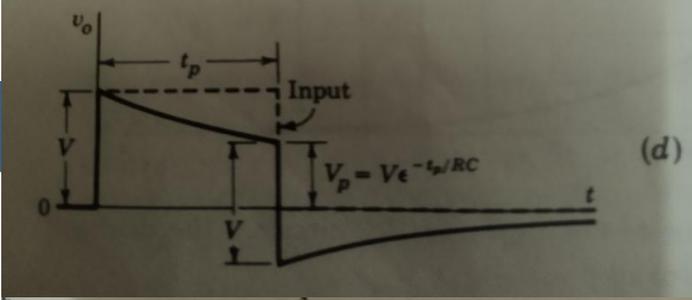
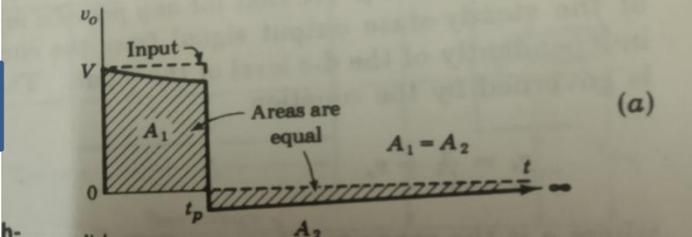
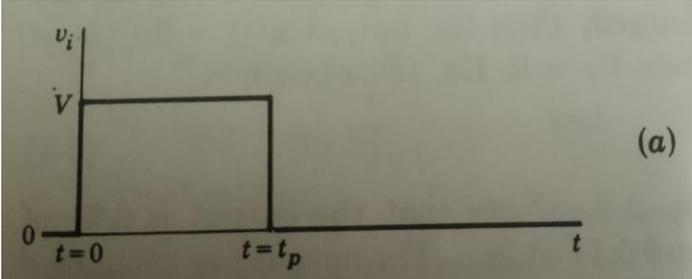
- $(V_0 = Ve^{-t/\tau})$
- at $t = t_p$,
 $V_0 = V_p - V$ ($V > V_p$)
- $V_0 = V(e^{-t_p/RC} - 1) Ve^{-(t-t_p)/RC}$

RC >> t_p

RC ~ t_p

- i) RC >> T_p
- ii) RC comparable with T_p
- iii) RC << T_p

RC << t_p





High pass circuit: Square wave Input

Square wave input:

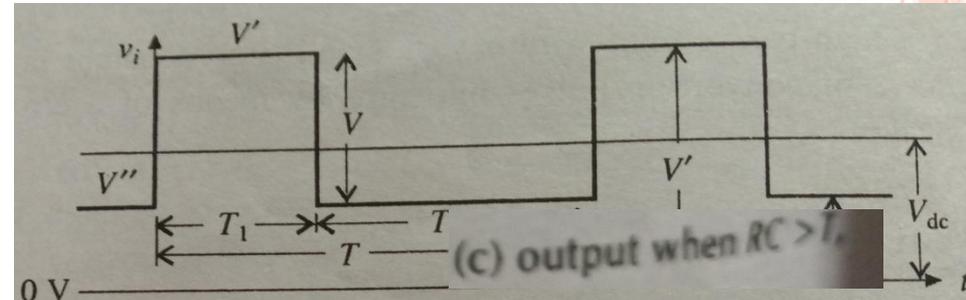
One constant level V' for $t = T_1$,
and at another constant level V''
for $t = T_2$

Which is repetitive with a period
 $T = T_1 + T_2$

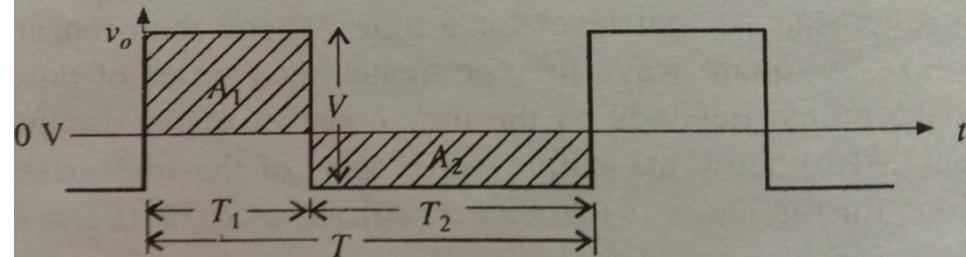
The response of RC high pass
circuit for

- i. $RC \gg T_1$ and $RC \gg T_2$,
ie $RC \gg T$

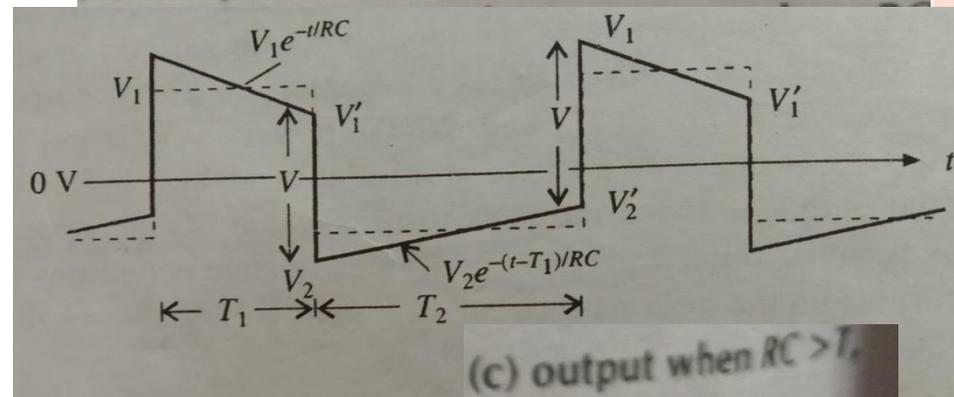
the output wave will be
identical to the input except
that the dc component will
be lacking (as an average
value is zero)



(a) A square wave input, i



(b) output when RC is arbitrarily large,



(c) output when $RC > T$,



High pass circuit: Square wave Input

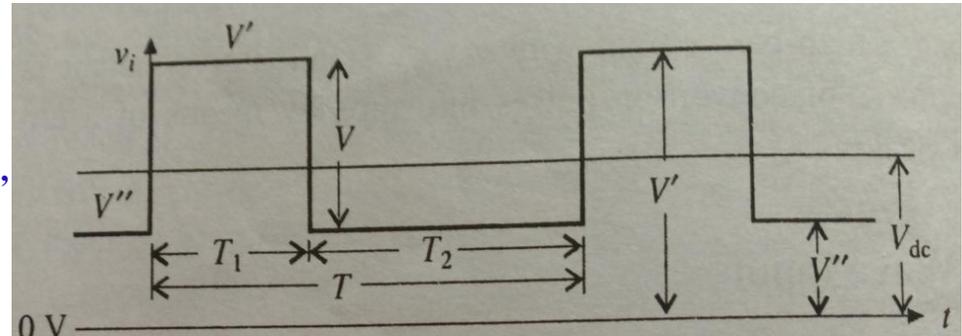
Square wave input:

ii. $RC \approx T_1$ and $RC \approx T_2$,
ie $RC \approx T$

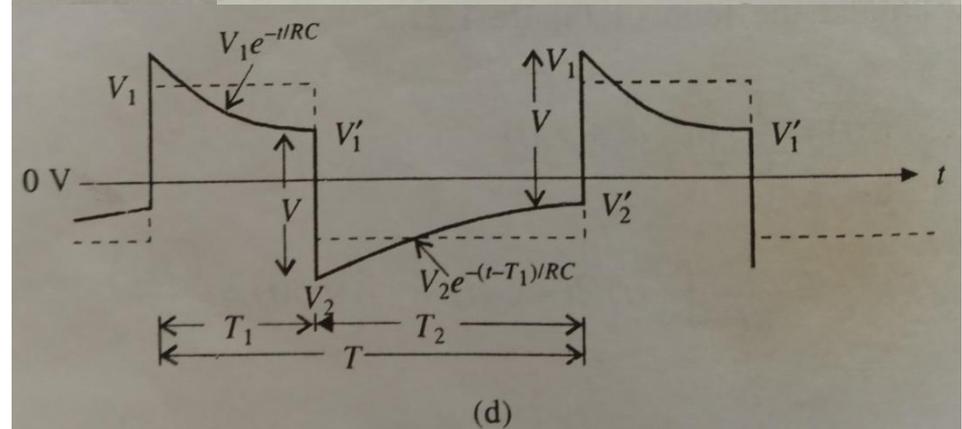
$$V_1' = V_1 e^{-T_1/RC},$$
$$V_1' - V_2 = V$$

$$V_2' = V_2 e^{-T_2/RC},$$
$$V_1 - V_2' = V'$$

iii.



(a) A square wave input, |



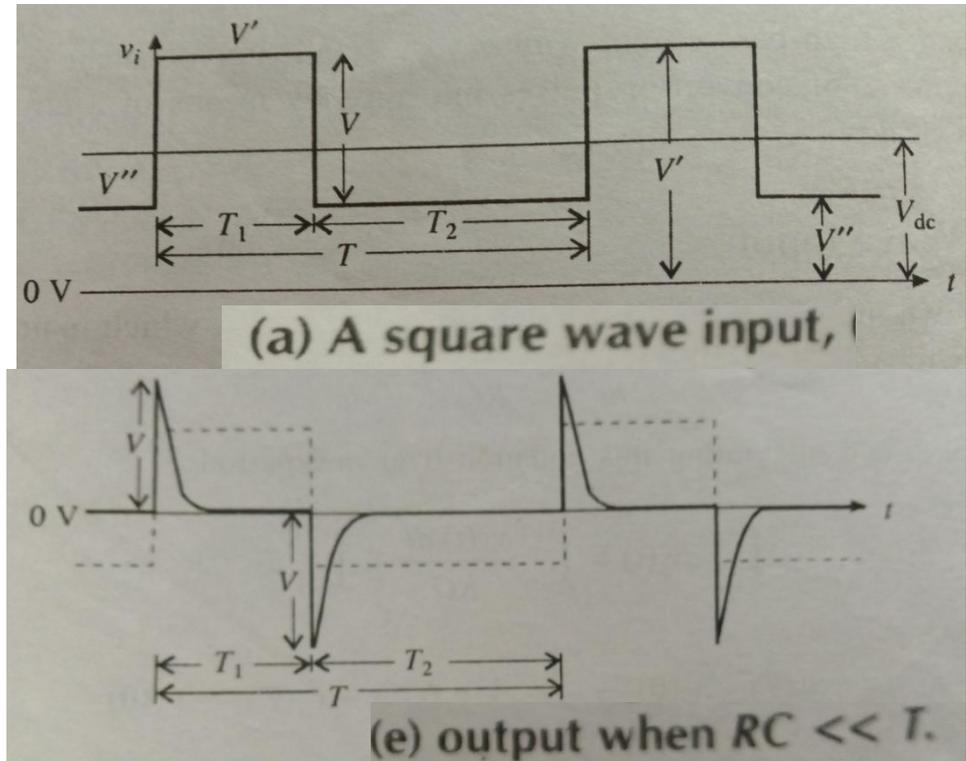
(d) output when RC is comparable to T ,



High pass circuit: Square wave Input

Square wave input:

- iii. $RC \ll T_1$ and $RC \ll T_2$
, ie $RC \ll T$
the output wave will consist of alternate +ve and -ve peaks, peak to peak amplitude of the output is double then the peak-to peak amplitude of the input





High pass circuit: Square wave Input

Square wave input:

i. $RC \gg T_1 \ \& \ RC \gg T_2$,
ie $RC \gg T$

ii. $RC \approx T_1 \ \& \ RC \approx T_2$,
ie $RC \approx T$

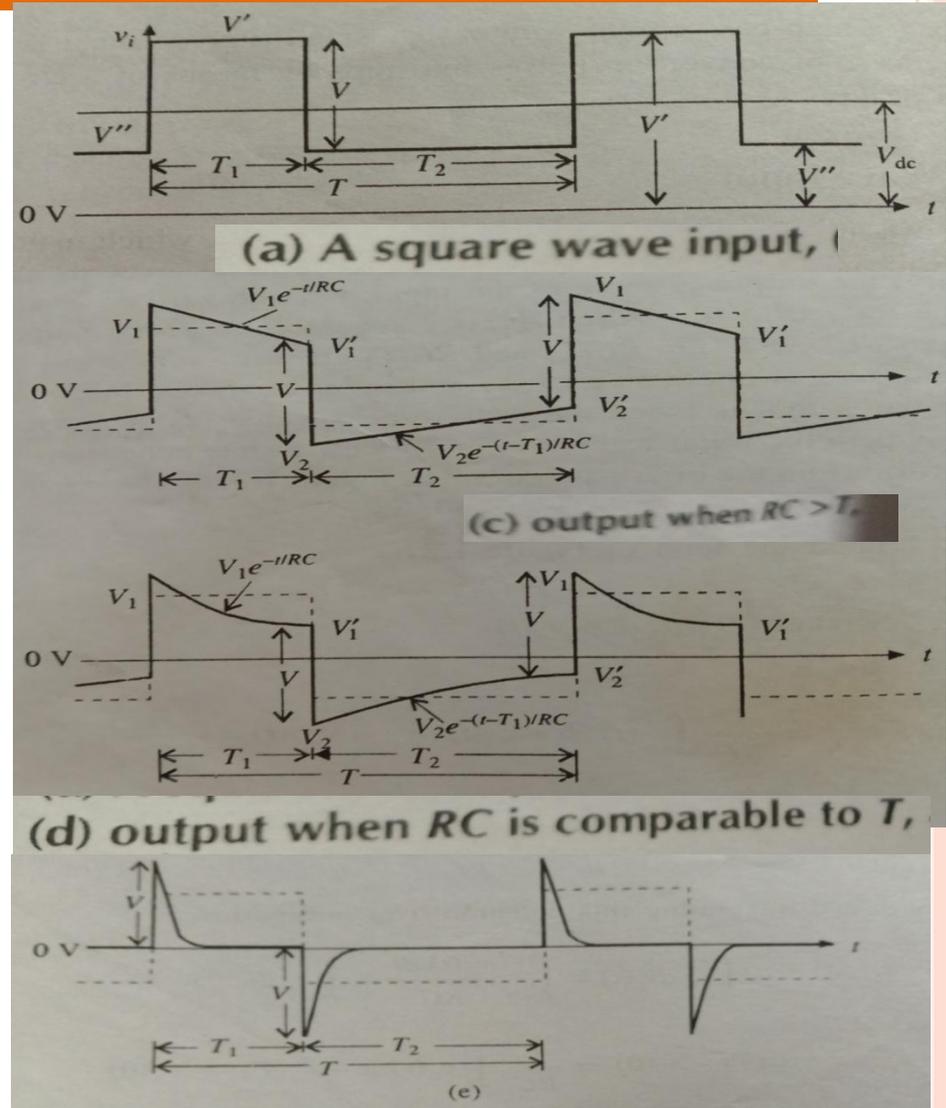
$$V_1' = V_1 e^{-T_1/RC},$$

$$V_1' - V_2 = V$$

$$V_2' = V_2 e^{-T_2/RC},$$

$$V_1 - V_2' = V$$

iii. $RC \ll T_1 \ \& \ RC \ll T_2$,
ie $RC \ll T$





High pass circuits: Pulse Input

cont...

When $\tau \ll t_p$ where $\tau = RC$

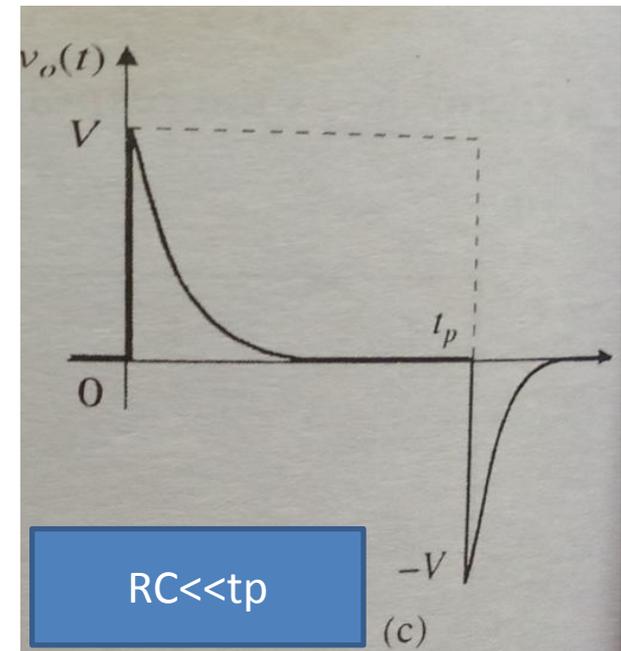
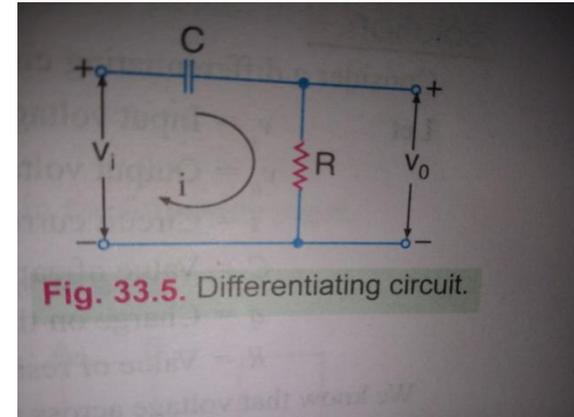
Pulse is converted into spikes

The process of converting pulses into spikes (pips) by means of RC circuit of very short time constant ($RC \ll t_p$) is called peaking circuit

Or

Differentiator

If the time constant is very very small as compare to the time required for the input signal to make an appreciable change, the circuit is called a differentiator





High pass circuits: Differentiating Circuit

cont...

$$V_o \propto \frac{dV_i}{dt}$$

High pass RC circuit as a Differentiator:

$$V_o = k \frac{dV_i}{dt}$$

If the time constant is very very small as compare to the time required for the input signal to make an appreciable change , the circuit is called a differentiator

Actually

When $\tau \ll t_p$ (where $\tau = RC$, $t_p = T$),

$V_R \ll V_C$ (for low freq X_c is high $X_c = \frac{1}{2\pi fC}$),

Therefore total input voltage V_i appears across capacitor C and hence the total current i is determined entirely by the Capacitor

$$i = C \frac{dV_c}{dt}$$

$$= C \frac{dV_i}{dt}$$

$$V_o \propto \frac{dV_i}{dt}$$

$$iR = RC \frac{dV_i}{dt}$$

$$V_o = RC \frac{dV_i}{dt}$$

Hence the output is proportional to the derivative of the input



High pass circuits: Sq.wave Input

cont...

When $\tau \ll t_p$ where $\tau = RC$
+ve Pulse and -ve Pulse is converted into spikes

The process of converting pulses into spikes (pips) by means of RC circuit of very short time constant ($RC \ll t_p$) is called peaking circuit

Or Differentiator

If the time constant is very very small as compare to the time required for the input signal to make an appreciable change, the circuit is called a differentiator

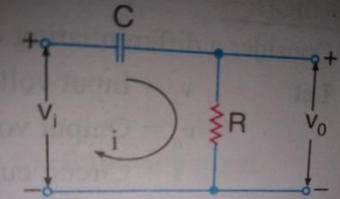
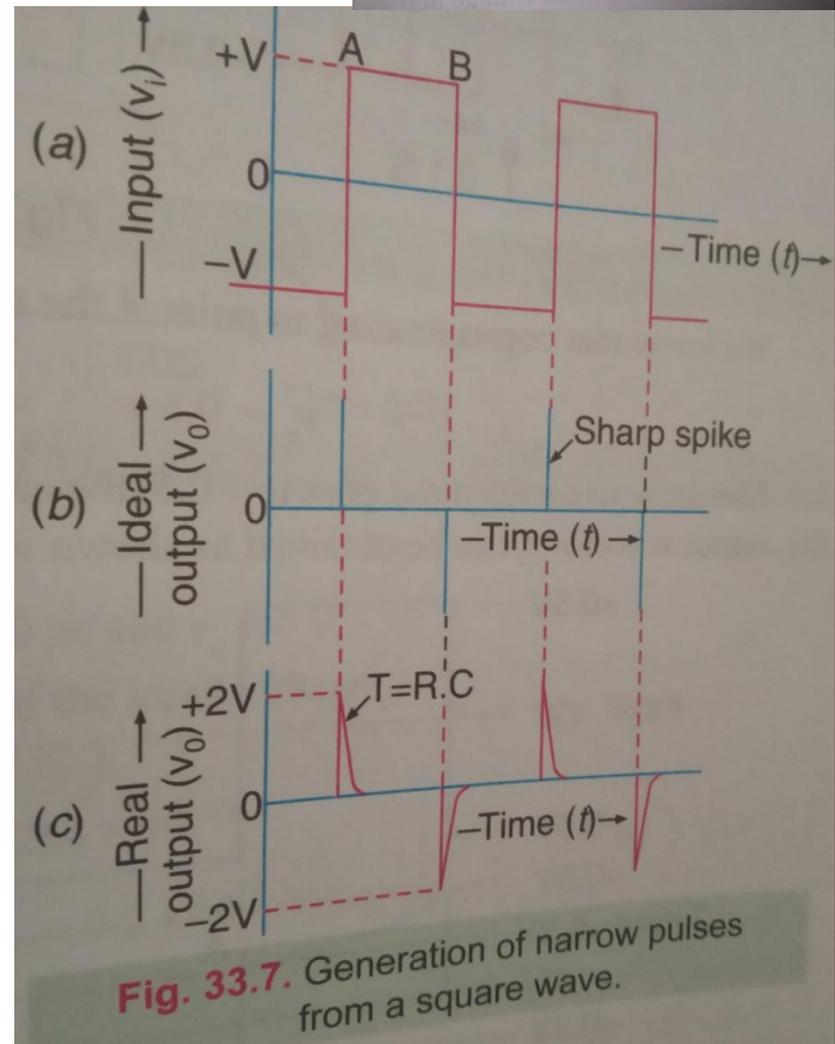
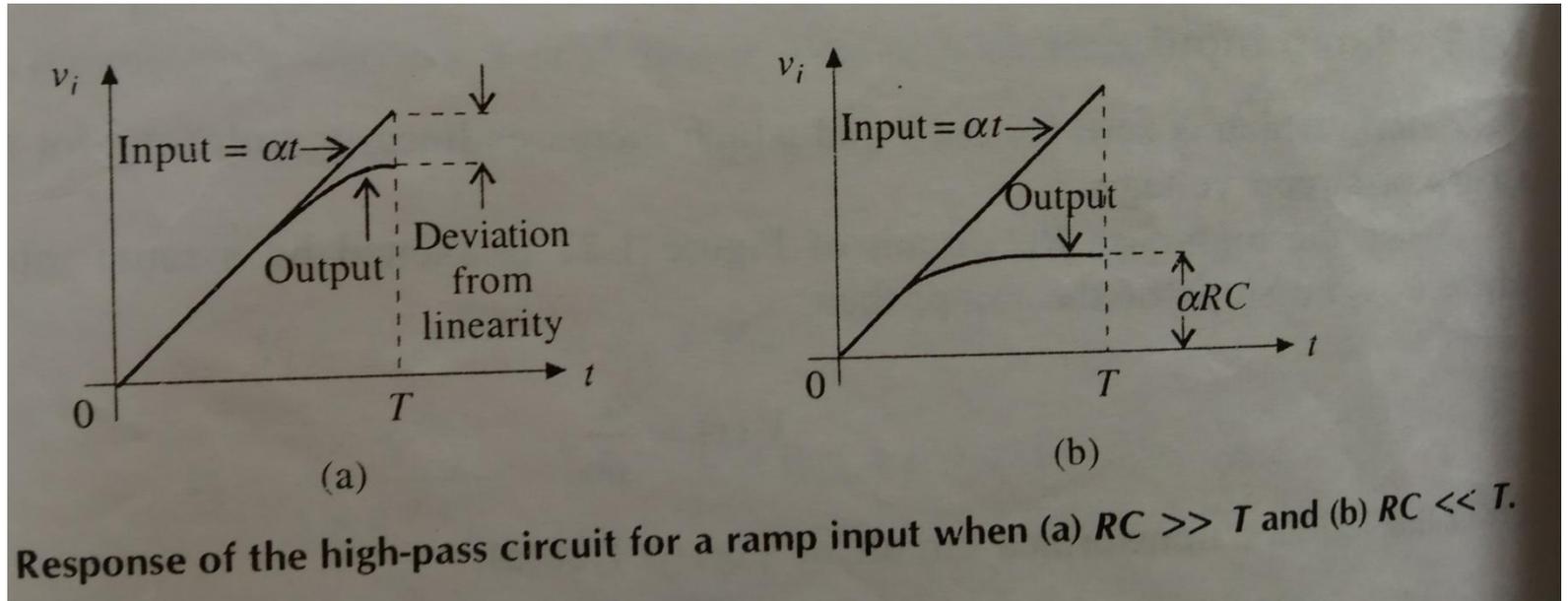


Fig. 33.5. Differentiating circuit.





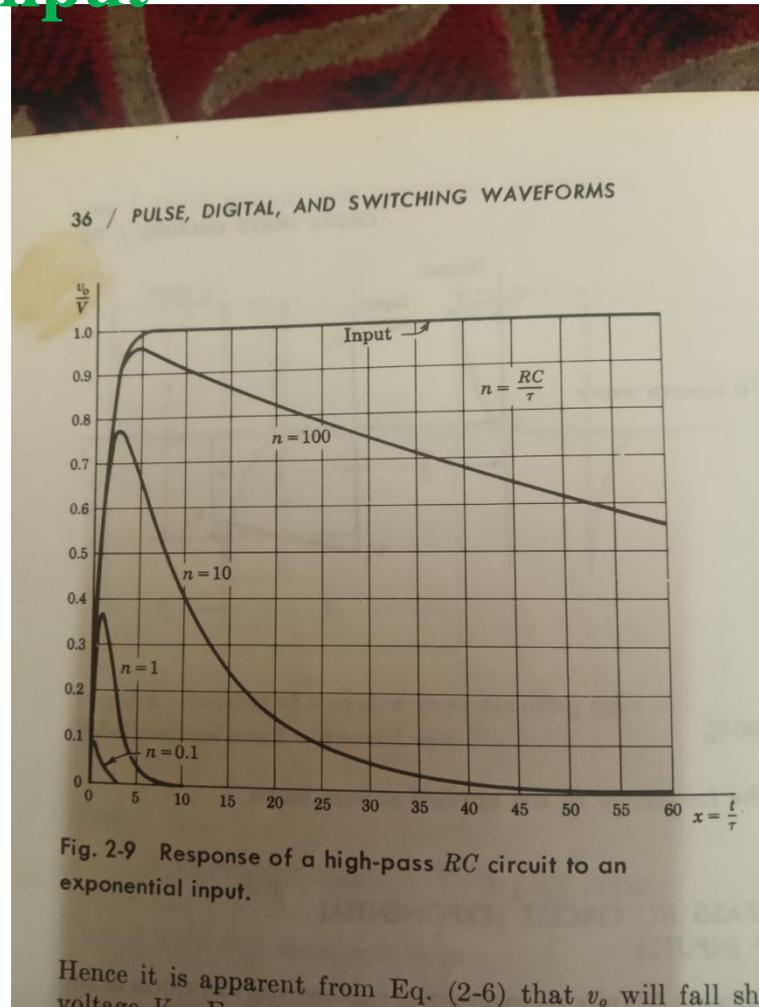
High pass circuits: Ramp Input





High pass circuits:

Response of High pass RC circuits for exponential input





Types of Wave shaping circuits

Types of Wave shaping circuits

- **Linear wave shaping circuits-**

- It use the transient properties of Resistors, Capacitors, Inductors to realize the mathematical operations of Integration & differentiation

- **Differentiating Circuit:**

$$V_o \propto \frac{dV_i}{dt}$$

$$V_o = k \frac{dV_i}{dt}$$

- It is realised by a simple RC series circuit
- Output is taken across R and $X_c \gg R$

$$X_c = \frac{1}{2\pi fC}$$

$$R \ll \frac{1}{2\pi fC}, \quad f \ll \frac{1}{2\pi RC}, \quad \frac{1}{T} \ll \frac{1}{2\pi RC}$$

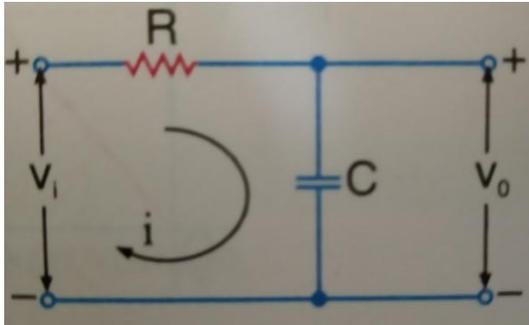
$$2\pi RC \ll T, \quad \tau \ll T \quad V_o = RC \frac{dV_i}{dt} = \tau \frac{dV_i}{dt}$$



Low pass RC circuits



Linear wave shaping circuits



- **Low pass RC circuits**
 - Low Pass Filter,
 - as an Integrator – $\tau (RC) \gg T$



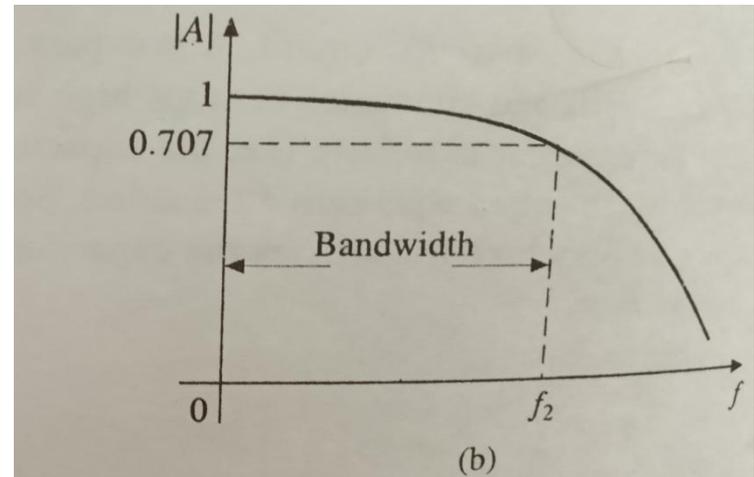
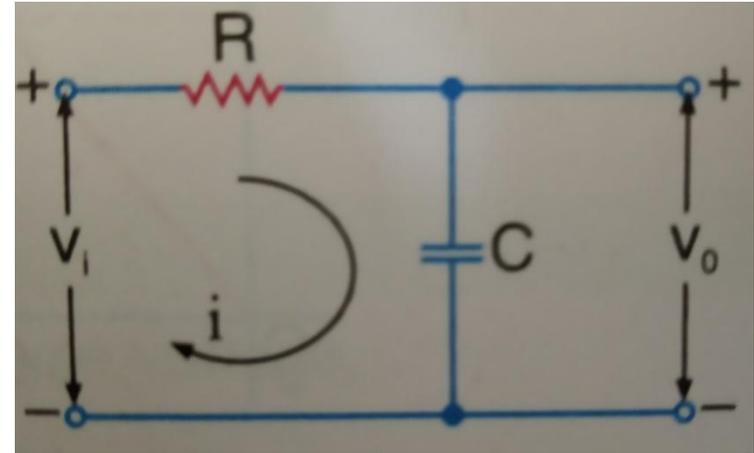
Linear wave shaping circuits

- **Low pass RC circuits**
 - Low pass filters
 - Use to perform functions of Integration, $\tau (RC) \gg T$

$$X_C = \frac{1}{2\pi fC}$$

$f = 0, f = \infty$ $X_C \rightarrow \infty, X_C \rightarrow 0$ resp

- as f increases, X_C decreases, o/p and magnitude of gain decreases
- low frequency components in the i/p signal appears at the o/p with less attenuation as compare to high frequency components
- For HF, capacitor acts as a short circuit and the o/p decreases to zero



low-pass RC circuit and (b) its frequency response.



Low pass RC circuits: Sinusoidal Input

1. Sinusoidal Input

Expression for the lower cutoff frequency-

- $V_i = V_m \sin \omega t$
- $i = V_i / (R - jX_c)$
- $V_o = i(-jX_c)$
 $= V_i * (-jX_c) / (R - jX_c)$

$$|A| = \left| \frac{V_o}{V_i} \right| = \frac{-jX_c}{R - jX_c} = \frac{1}{R/jX_c - 1}$$

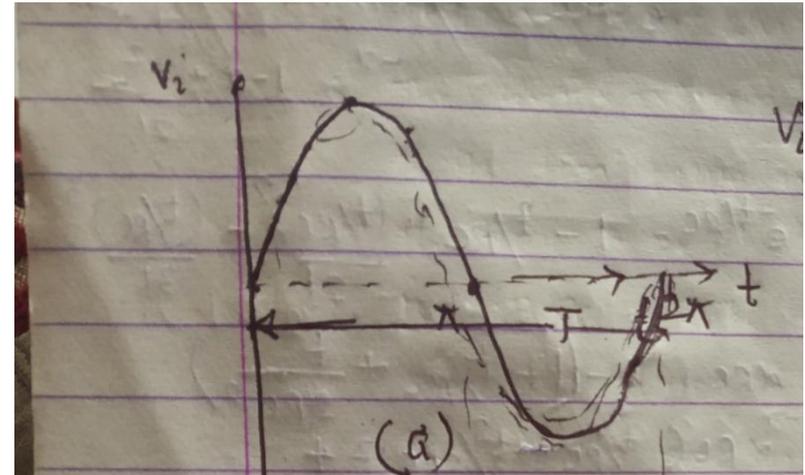
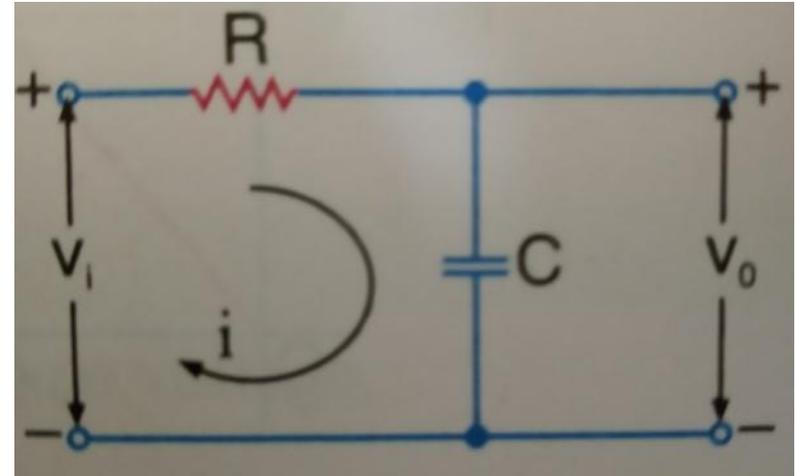
$$\left| \frac{V_o}{V_i} \right| = |A| = \frac{1}{\sqrt{1 + (R/X_c)^2}}$$

$$= \frac{1}{\sqrt{1 + (f/f_2)^2}}$$

$$\theta = -\tan^{-1} \frac{f}{f_2}$$

$$f_2 = \frac{1}{2\pi RC}$$

3db lower cutoff frequency





Low pass RC circuits: Sinusoidal Input

1. Sinusoidal Input

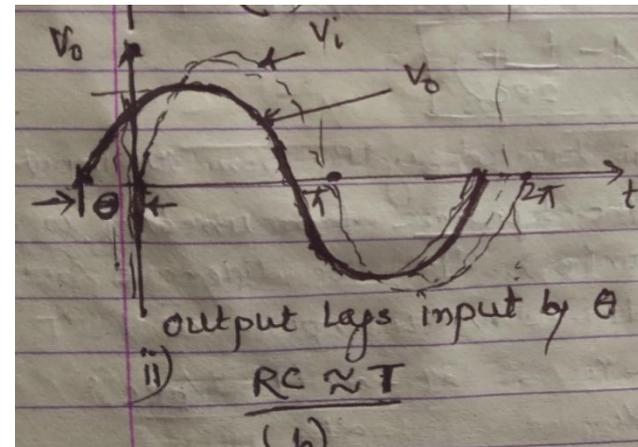
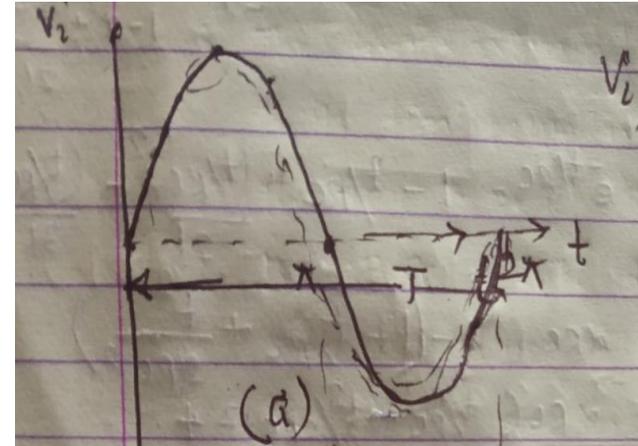
$$\left| \frac{V_o}{V_i} \right| = |A| = \frac{1}{\sqrt{1 + (R/X_c)^2}}$$
$$= \frac{1}{\sqrt{1 + (f/f_2)^2}}$$

$$\theta = -\tan^{-1} \frac{f}{f_2}$$

$$f_2 = \frac{1}{2\pi RC}$$

- Sinusoidal Input (V_i)
- Sinusoidal output (V_o)

Output waveform Nature is same but amplitude reduced and output lags input by θ





Low pass RC circuits: Sinusoidal Input

1. Response of Low pass RC circuit for Sinusoidal Input with Various circuit time constant(RC)

$$\left| \frac{V_o}{V_i} \right| = |A| = \frac{1}{\sqrt{1 + (R/X_c)^2}}$$

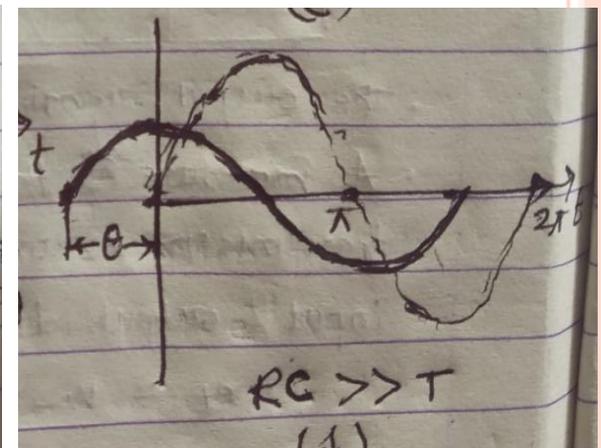
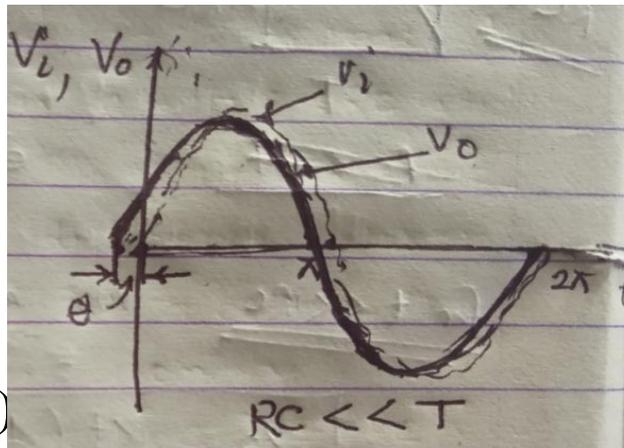
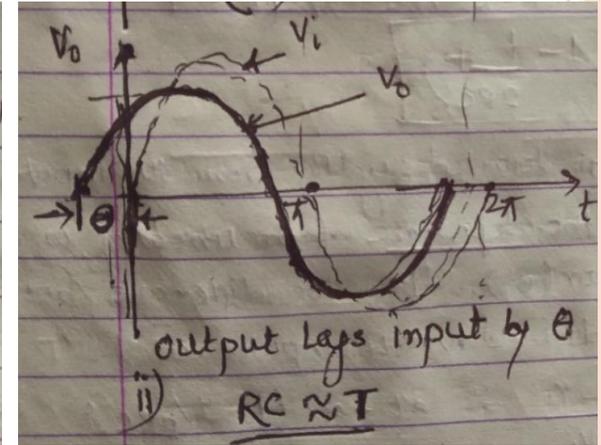
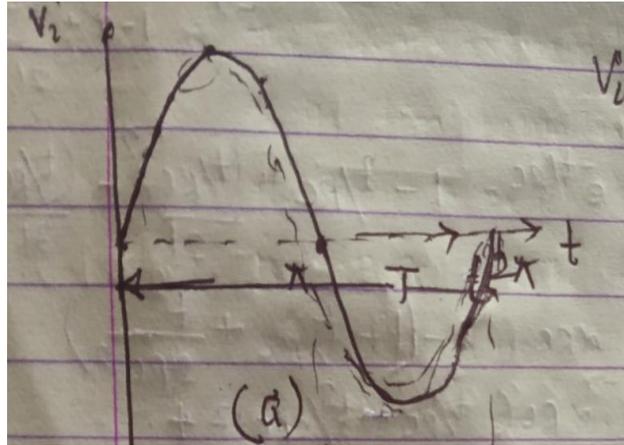
$$= \frac{1}{\sqrt{1 + (f/f_2)^2}}$$

$$\theta = -\tan^{-1} \frac{f}{f_2}$$

$$f_2 = \frac{1}{2\pi RC}$$

Input- V_i (fig.a)
Output- V_o

- b. $RC \ll T$, (low f)
- c. $RC \approx T$, ($f = f_2$)
- d. $RC \gg T$ (High f)





Low pass circuits: Step Input

2. Step Input

$V_i = 0, t < 0$ and $V_i = V, t > 0$

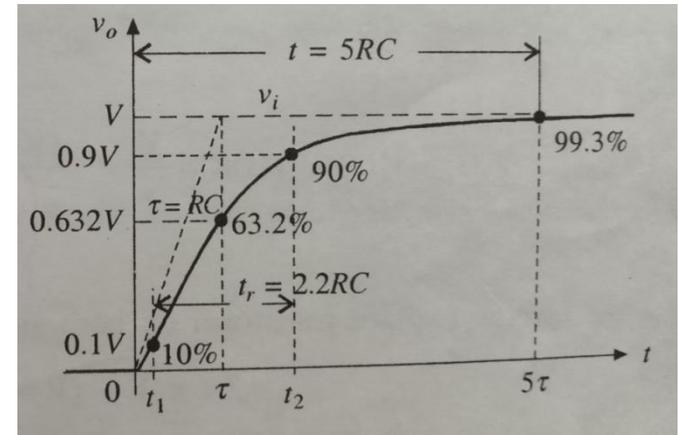
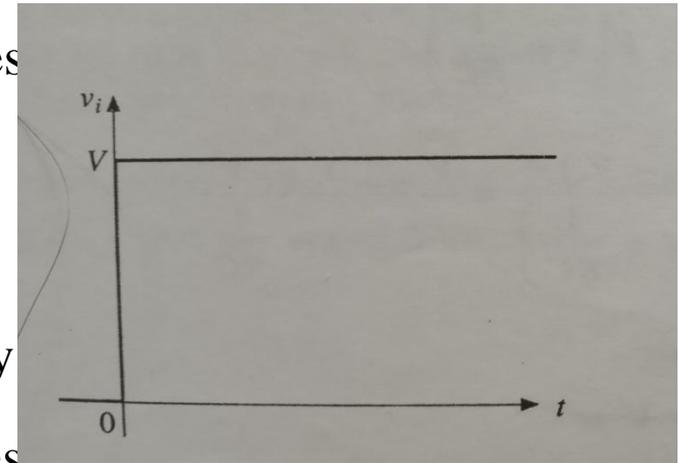
The transition between two voltage levels takes place at $t = 0$, Voltages at ($t=0+$, $t=0-$)

▪ The response of low pass RC circuit is exponential with time constant $RC = \tau$ since the V_c cannot change instantaneously

▪ The output ($V_0 = V_c$) starts from zero and rises towards the steady state value V ,
 $V_0 = V_f = V$,

▪ The initial value of V_0 at $t=0$
 $V_0 = V_i = 0$

$$\begin{aligned}
 V_0 &= V_f + (V_i - V_f) e^{-t/\tau} \\
 &= V + (0 - V) e^{-t/\tau} \\
 &= V(1 - e^{-t/\tau})
 \end{aligned}$$



$$\begin{aligned}
 \text{Rise time } t_r &= 2.3RC - 0.1RC = 2.2 RC \\
 &= 0.35/f_2
 \end{aligned}$$



Low pass circuits: Pulse Input

3. Pulse Input

- If the pulse input is applied to low pass RC circuit then Response

i) for $t < t_p$ is similar to that for step input voltage and $V_{o1} = V(1 - e^{-t/\tau})$

ii) At the end of pulse i/p falls abruptly by an amount V but the capacitor voltage cannot change instantaneously for finite current flow therefore output decreases exponentially

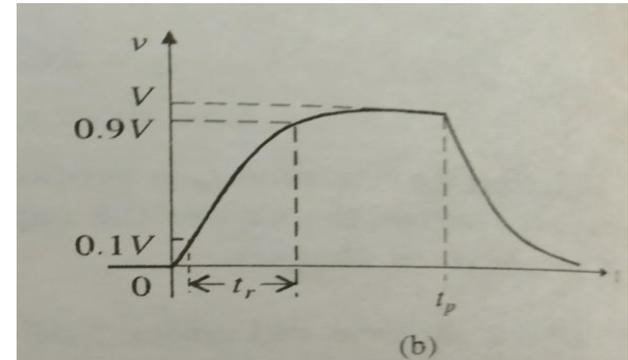
$$\text{at } t = t_p, V_{o1} = V_p = V(1 - e^{-t_p/\tau})$$

iii) At $t > t_p$ capacitor discharges exponentially,

$$\text{at } t = t_p, V_o = V(1 - e^{-t_p/\tau})$$

after t_p ($t > t_p$) the output V_o decreases exponentially to zero from $V_0 = V_p$ with time constant RC For $t > t_p$,

$$\begin{aligned} V_{o2} &= 0 + (V_p - 0) e^{-(t-t_p)/RC} \\ &= V_p e^{-(t-t_p)/RC} \end{aligned}$$





Low pass circuits: Pulse Input

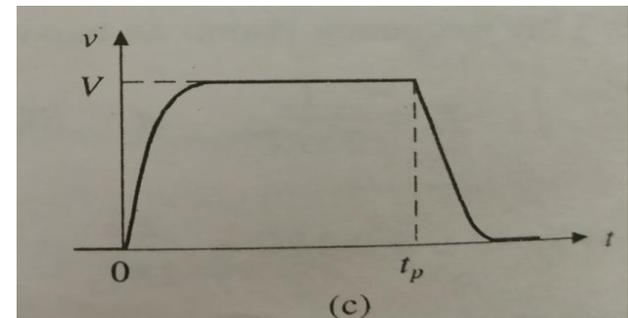
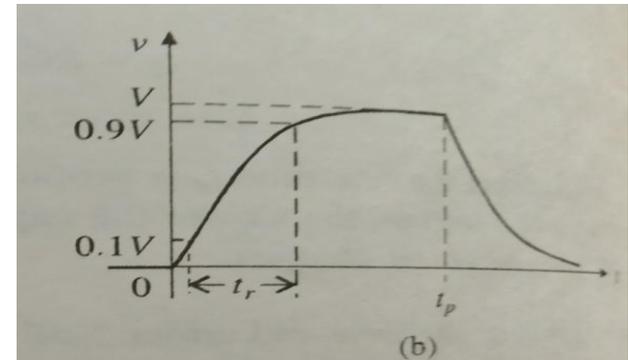
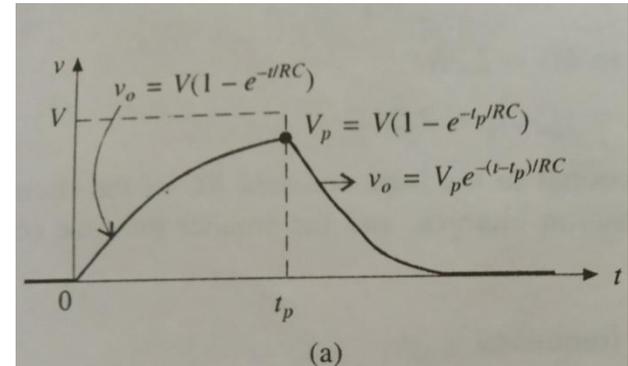
3. Pulse Input

- Response of low pass RC circuit for pulse input with various RC

i) $RC \gg T_p$ (high f)

ii) $RC = T_p$

iii) $RC \ll T_p$ (low f)





Low pass circuit: Square wave Input

Square wave input:

level V' for $t = T_1$, & level V'' for $t = T_2$
Which is repetitive with a $T = T_1 + T_2$

The response of RC low pass circuit for

i. For T_1 , the equation for rising portion

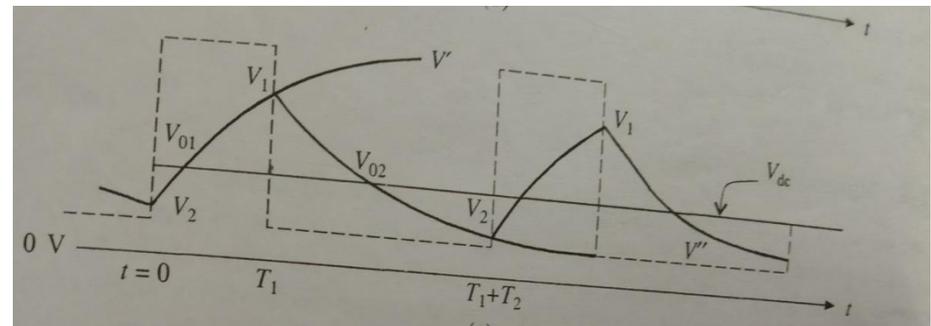
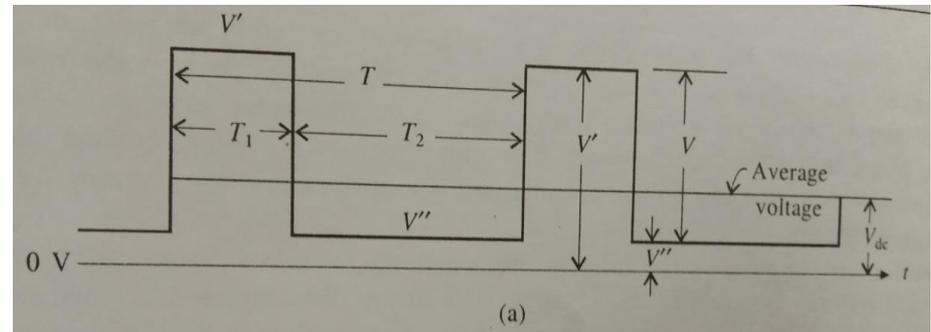
$$V_{01} = V' - (V' - V_2) e^{-t/RC}$$

Where $V_2 = V_c$ at $t = 0$, and V' is the level upto which capacitor may charge

ii. For T_2 , the equation for falling portion

$$V_{02} = V'' - (V'' - V_1) e^{-(t-T_1)/RC}$$

Where $V_1 = V_c$ at $t = T_1$, & V'' is the level upto which capacitor may charge



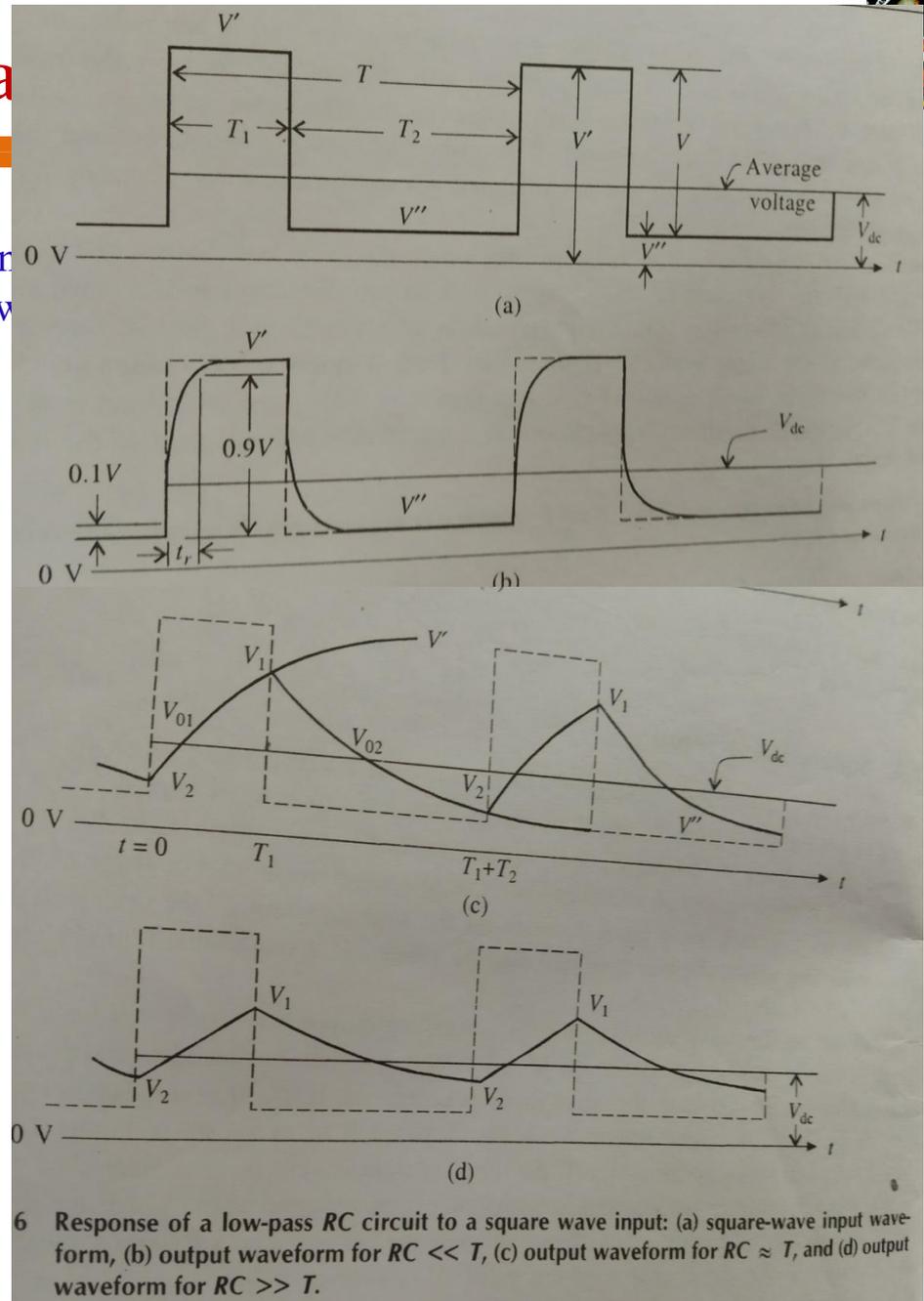
Low pass circuit: Square

Square wave input:

One constant level V' for $t = T_1$, & at another level V'' for $t = T_2$ Which is repetitive with Time period $T = T_1 + T_2$

The response of RC low pass circuit for

- i. $RC \ll T_1$ & $RC \ll T_2$, ie $RC \ll T$
- ii. $RC \approx T_1$ & $RC \approx T_2$, ie $RC \approx T$
- iii. $RC \gg T_1$ & $RC \gg T_2$, ie $RC \gg T$





Low pass circuits: Integrating Circuit

Low pass RC circuit
as an Integrator:

$$V_o \propto \int V_i dt$$

$$V_o = k \int V_i dt$$

If the circuit time constant is very large as compare to the time required for the input signal to make an appreciable change , the circuit is called an integrator

Actually

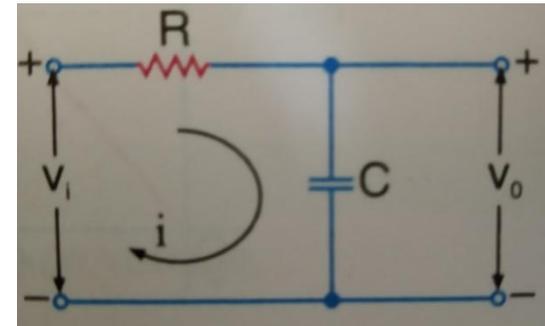
When $\tau \gg t_p$

(where $\tau = RC$, $t_p = T$),

$$V_c \ll V_R$$

(for high freq X_c is small $X_c = \frac{1}{2\pi fC}$),

Therefore total input voltage V_i appears across resistor R and hence the total current i is determined entirely by the resistor



$$V_i = V_R + V_C = V_R$$

$$i = \frac{V_R}{R} = \frac{V_i}{R}$$

$$V_o = \frac{1}{C} \int_0^T i dt$$

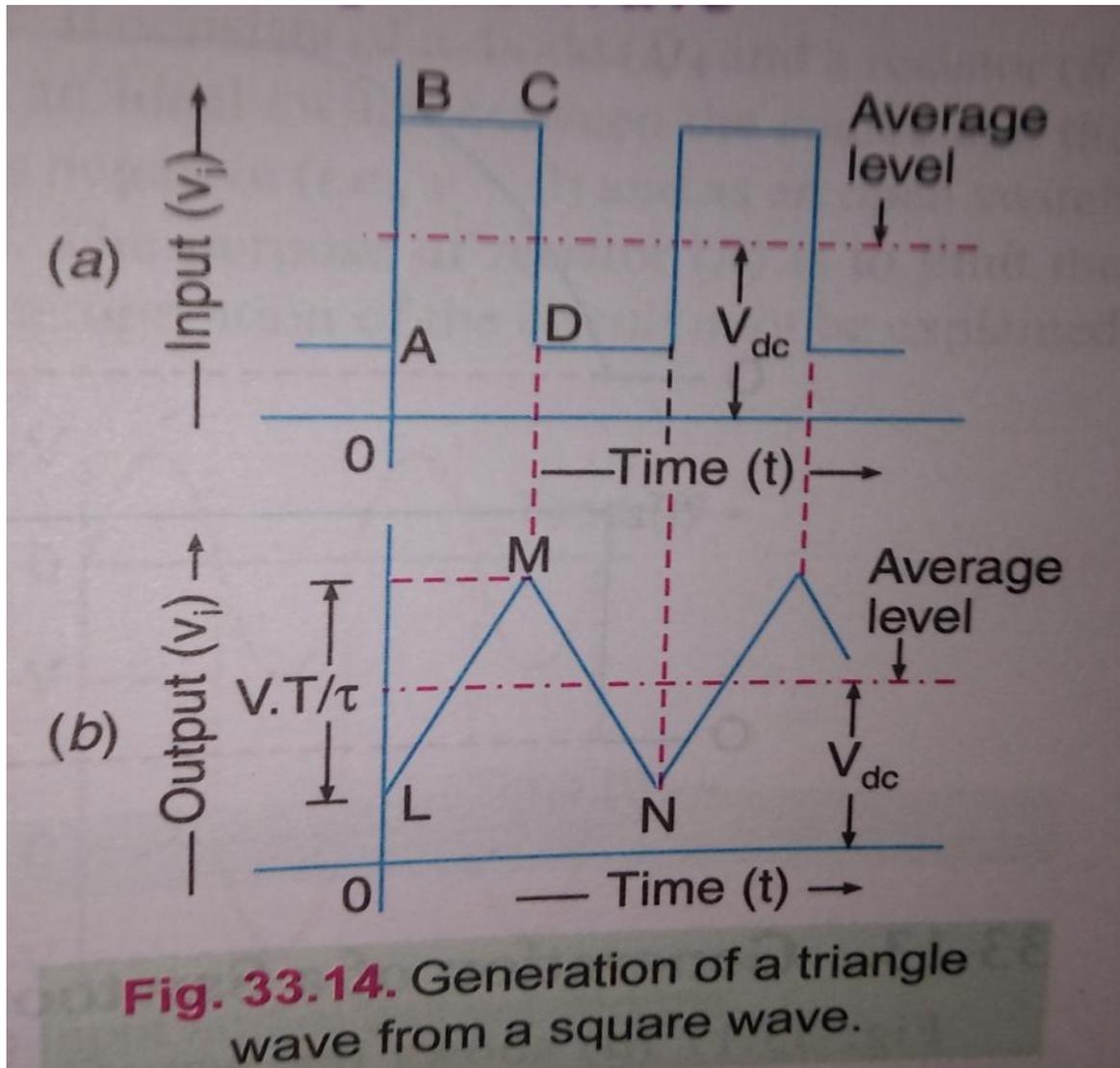
$$= \frac{1}{RC} \int_0^T V_i dt$$

$$\text{so } V_o \propto \int_0^T V_i dt$$

Hence the o/p(V_o) is proportional to the integration of the input(V_i)

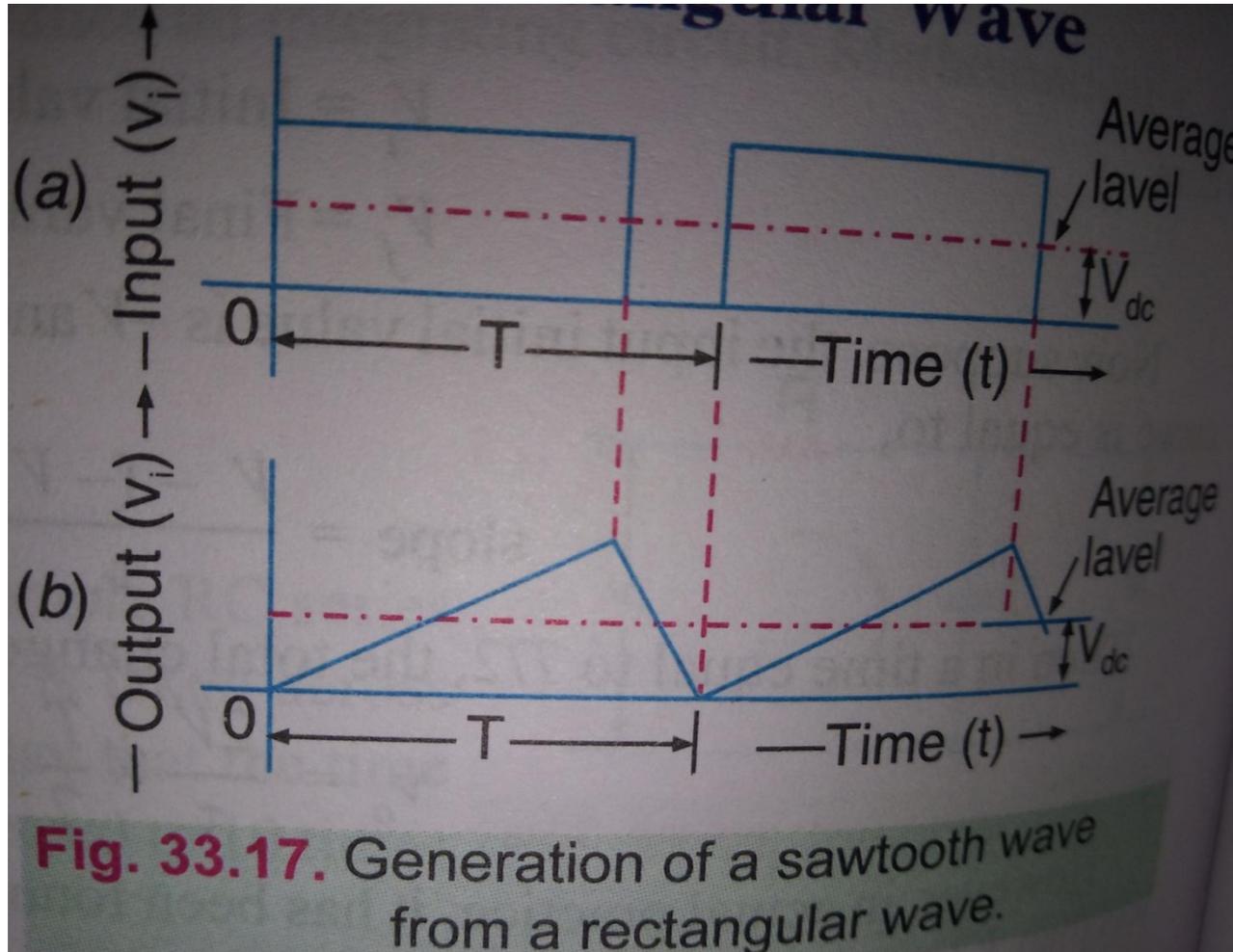


RC circuits



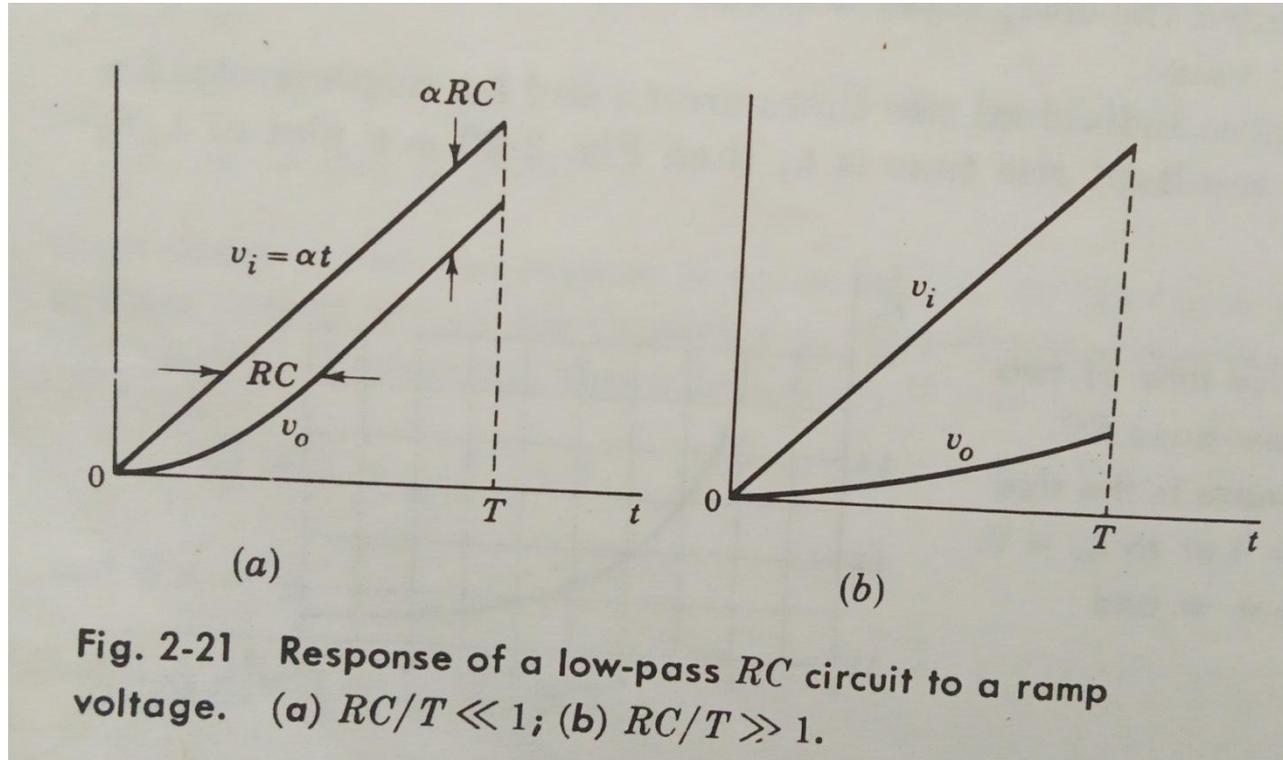


RC circuits





Low pass RC circuits: ramp Input



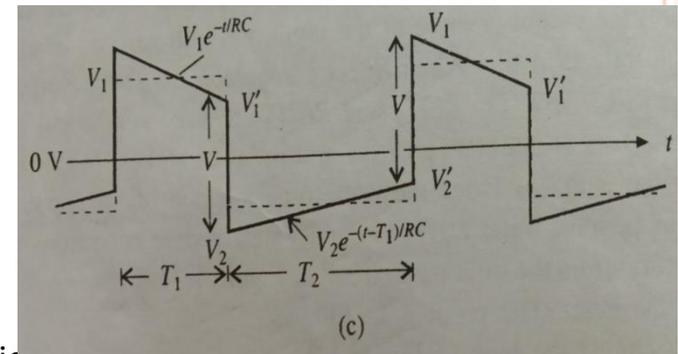
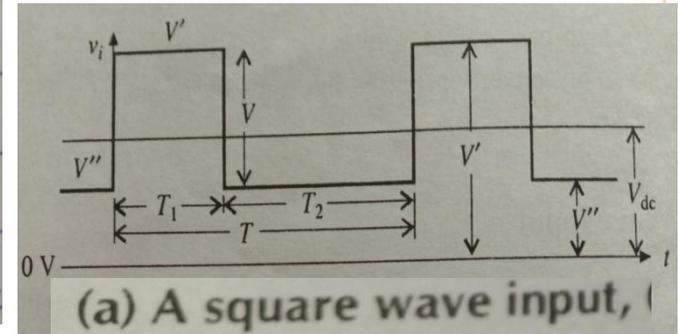
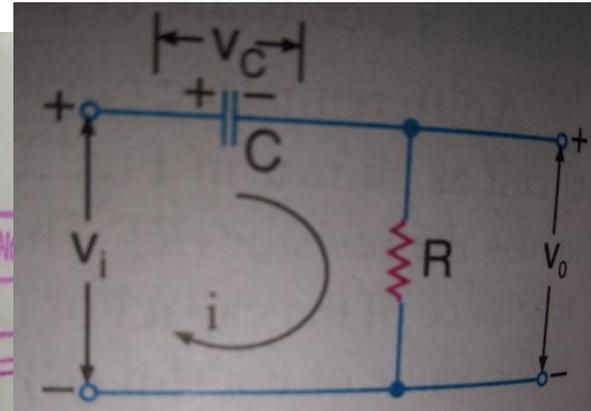


Problem on High Pass RC circuits

* Expression for the % tilt
 Define % tilt occurring in the output waveform after transmission of symmetrical sq. wave through RC high pass circuit and then show that -

$$\% \text{ tilt} \cong p \cong \frac{T}{2RC} \times 100 \text{ or } p \cong \pi f_1 / f \times 100.$$

Defⁿ:
$$\% \text{ tilt} = \frac{V_1 - V_1'}{V/2} \times 100$$





Problem on High Pass RC circuits

linear when $RC \gg T$

for symmetrical square wave
 $T_1 = T_2 = T/2$ and because of
the symmetry $V_1 = -V_2$ and $V_1' = -V_2'$

If $RC \gg T$ and the response to a
sq. wave have the appearance as shown
in fig. and we got the equations as
follows.

$$V_1' = V_1 e^{-T_1/RC} \quad \& \quad V_1' - V_2 = V \quad \text{--- (1)}$$
$$V_2' = V_2 e^{-T_2/RC} \quad \& \quad V_1 - V_2' = V \quad \text{--- (2)}$$



RC circuits

$$V_1' = V_1 e^{-T_1/RC} \quad \& \quad V_1' - V_2 = V \quad \text{--- (1)}$$

$$V_2' = V_2 e^{-T_2/RC} \quad \& \quad V_1 - V_2' = V \quad \text{--- (2)}$$

for symmetrical sq. wave eqⁿ (1) becomes

$$V_1' = V_1 e^{-T/2RC}$$

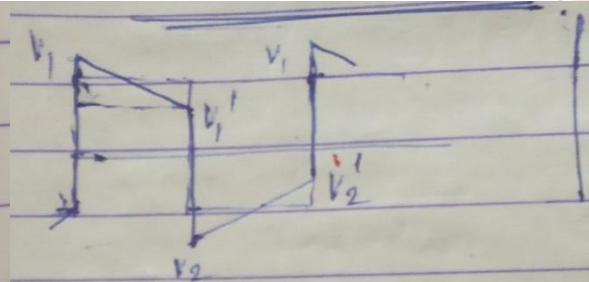
$$V_1' - V_2 = V$$

or $V_1' = V + V_2 = V - V_1$ \downarrow $V_2 = -V_1$

$$\begin{matrix} T_1 = T_2 = T/2 \\ V_1 = -V_2 \quad \& \quad V_1' = -V_2' \end{matrix}$$

$$\therefore V - V_1 = V_1 e^{-T/2RC}$$

$$\boxed{V_1 = \frac{V}{1 + e^{-T/2RC}}} \quad \text{(3)}$$



for symmetrical square wave

$$T_1 = T_2 = T/2 \quad \& \quad \text{a}$$

the symmetry $V_1 = -V_2$

If $RC \gg T$ and the



RC circuit

similarly

$$V_1' = V_1 e^{-T/2RC}$$

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$$V_1' - V_2 = V \text{ or } V_1' = V + V_2 = V - V_1' \text{ or } V_1 = \underline{V - V_1'}$$

$$\therefore V_1' = (V - V_1') e^{-T/2RC}$$

$$V_1' = \frac{V e^{-T/2RC}}{1 + e^{-T/2RC}} = \frac{V}{1 + e^{T/2RC}}$$

$$\boxed{V_1' = \frac{V}{1 + e^{T/2RC}} \quad \text{--- (4)}}$$

for $\underline{2RC \gg T}$ or $\underline{T/2 \ll RC}$

$$V_1 = \frac{V}{1 + e^{T/2RC}}$$

$$(e^{-x} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} \dots)$$

$$e^{T/2RC} = 1 + \frac{T/2RC}{1} + \frac{(T/2RC)^2}{2!} + \dots$$



RC circuit

$$\frac{V_1}{V} = \frac{1}{1 + e^{T/2RC}} \quad \text{--- (4)}$$

for $2RC \gg T$ or $T/2 \ll RC$

$$V_1 = \frac{V}{1 + e^{T/2RC}} \quad \text{--- (5)}$$

$$(e^{-x} = 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots)$$

$$e^{-T/2RC} \approx 1 - \frac{T}{2RC} + \frac{(T/2RC)^2}{2!} - \dots$$

for $T/2 \ll RC$ eliminate higher order terms

$$\therefore e^{-T/2RC} \approx (1 - T/2RC) \quad \text{--- (3)}$$

$$\therefore V_1 = \frac{V}{1 + 1 - T/2RC} = \frac{V}{2(1 - T/4RC)} = \frac{V(1 - T/4RC)^{-1}}{2}$$

$$(1 - T/4RC)^{-1} = 1 + \frac{T}{4RC} + \left(\frac{T}{4RC}\right)^2 + \dots$$

{ Binomial expansion }

$$\approx (1 + T/4RC)$$

$$\therefore V_1 = \frac{V}{2} \left(1 + \frac{T}{4RC}\right) \quad \text{--- (5)}$$



RC circ

from eqⁿ (4)

$$V_1' = \frac{V}{1 + e^{T/2RC}}$$

$$(e^x = 1 + x + \frac{x^2}{2!})$$

$$e^{T/2RC} = 1 + T/2RC + \frac{(T/2RC)^2}{2!} + \dots$$

$$\approx (1 + T/2RC)$$

$$V_1' = \frac{V}{1 + 1 + T/2RC} = \frac{V}{2(1 + T/4RC)} = \frac{V(1 + T/4RC)^{-1}}{2}$$

$$(1 + x)^{-1} = 1 - x + x^2 - x^3 + \dots$$
$$(1 + T/4RC)^{-1} = 1 - T/4RC + \dots$$
$$\approx (1 - \frac{T}{4RC})$$

$$\therefore V_1' = \frac{V}{2} (1 - \frac{T}{4RC}) \quad \text{--- (5)}$$

$$\% \text{ tilt} = P = \frac{V_1 - V_1'}{V/2} \times 100$$

from eqⁿ (5) & (6)

$$P \equiv \frac{V(1 + T/4RC) - V(1 - T/4RC)}{V/2}$$

$$V_0 = 2V_{ipp}$$

$$T (T = T_1 + T_2)$$
$$T_1 = RC / \pi$$



RC circ

$$P \equiv \frac{T}{2RC} \times 100$$

% tilt

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$f_1 =$ lower 3dB frequency $f = 1/2RC$

$$\therefore 2RC = 1/\pi f_1 \quad \& \quad T = 1/f$$

$$\therefore P \equiv \frac{\pi f_1}{f} \times 100$$



THANKS A LOT

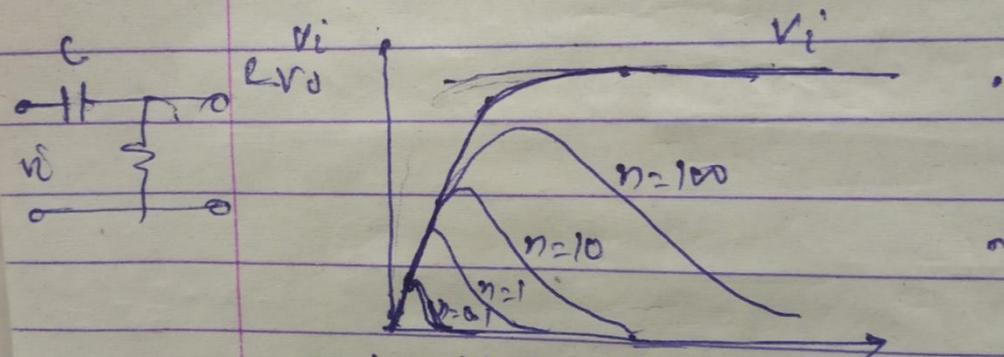


Thanks a lot



RC circuit

be narrower, but the
 will remain equal to the
 the input square wave, pro
 has vertical sides which is
 impossible, and therefore
rise time of the input
be taken into account.



$v_o(\text{initial}) = 0$ because $v_i = 0$
 at $t = 0$, then $v_o(0) = 0$

$$v_i = \int \frac{dq}{C} dt + v_o$$

$$\frac{dv_i}{dt} = \frac{v_o}{RC} + \frac{dv_o}{dt}$$

$$v_i = \frac{q}{C} + v_o$$

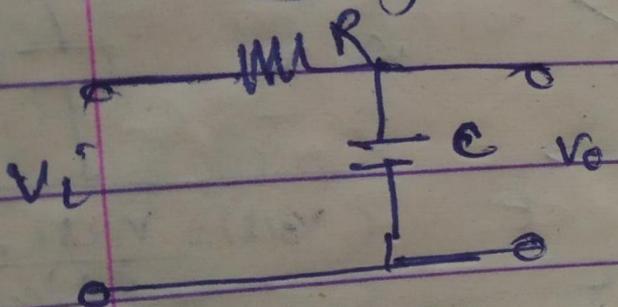
$$i = \frac{dq}{dt} = \frac{1}{C} \frac{dq}{dt}$$

$$\frac{dv_i}{dt} = \frac{1}{C} \frac{dq}{dt} + \frac{dv_o}{dt}$$

$$= \frac{i}{C} + \frac{dv_o}{dt}$$

The Low pass RC circuit as An

Integrator



$RC \gg T$

The time constant (RC) is very large in comparison with the time required for the input signal to make an appreciable change,

the ckt is called an integrator.

when $RC \gg T$ the voltage drop across C will be very small in comparison to the drop across R.

$(V_C \ll V_R)$

$V_i = V_R + V_C \approx V_R$

RC >> T

to make an approximation of

the ckt is called an integrator.

when $RC \gg T$, the voltage drop across C
will be very small in comparison to the drop
across R. ($V_C \ll V_R$)

$$V_i = V_R + V_C \approx V_R$$

$$\therefore i = V_R / R = V_i / R$$

$$V_o = \frac{1}{C} \int i dt$$

$$V_o = \frac{1}{RC} \int V_i dt$$

$$V_o \propto \int V_i dt$$

$$V_i = \alpha t, \quad V_o = \frac{\alpha t^2}{2RC}$$

$$\text{for } \alpha \text{ input } V_o = V_i - V_R = \alpha t - \alpha RC(1 - e^{-t/RC})$$

$$v_i \propto t, \quad v_o \propto \frac{t^2}{2RC}$$

for Ramp Input

$$v_o = v_i - V_R = \alpha t - \alpha RC(1 - e^{-t/RC})$$

$$v_o = \alpha t - \alpha RC [1 - (1 - t/RC + t^2/2(RC)^2 - \dots)]$$

$$= \alpha t - \alpha RC (t/RC - t^2/2(RC)^2)$$

$$= \alpha t - \alpha t + \alpha t^2/2RC$$

$$v_o = \frac{\alpha t^2}{2RC}$$

& $v_o = \frac{1}{RC} \int v_i dt = \frac{1}{RC} \int \alpha t dt$

$$= \frac{\alpha}{RC} \int t dt = \frac{\alpha t^2}{2RC}$$

$$v_o \propto \frac{t^2}{2RC}$$